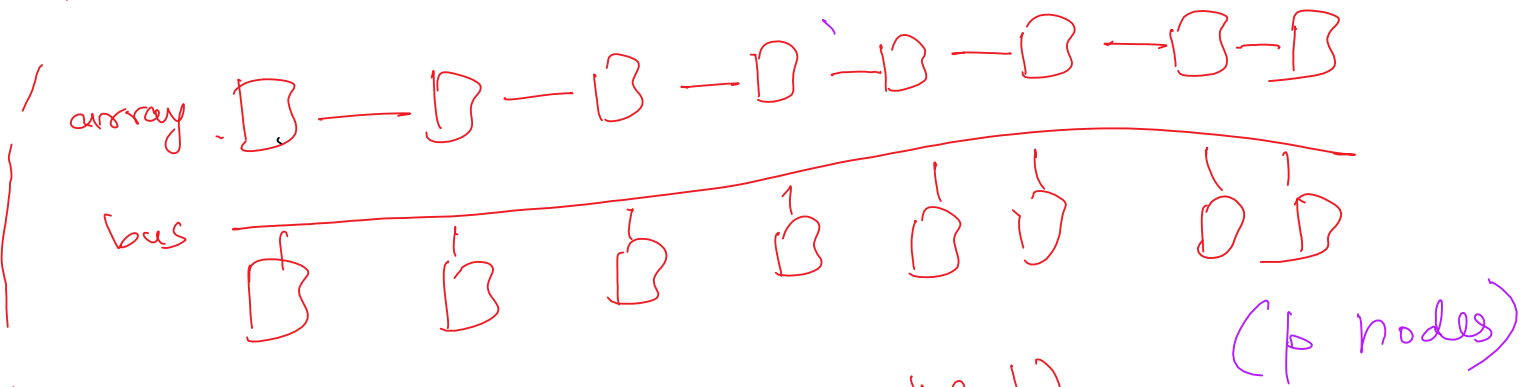


# Network Topologies

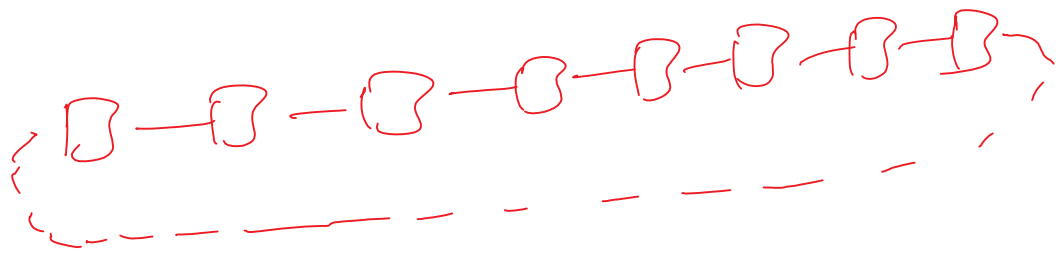
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## Array / bus Topology :



- diameter =  $p-1$  (terrible!)
- bisection bandwidth = 1 (terrible!)
- # links / node = 2 (great!)

## Ring topology :



- diameter  $\approx p/2$  ✓ (still terrible!)
- Bisection bw = 2
- # links per node = 2

# Mesh

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## 3) Mesh Topology:

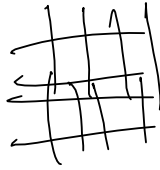
diameter:

✓  $(\sqrt{p}-1) \times 2$

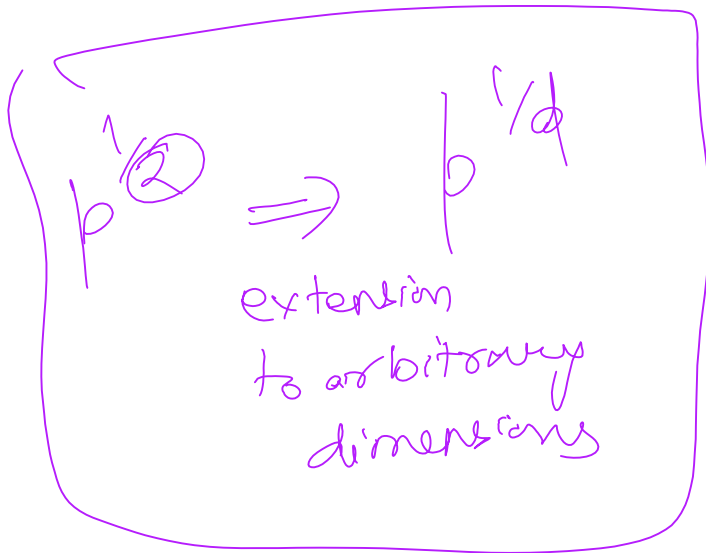
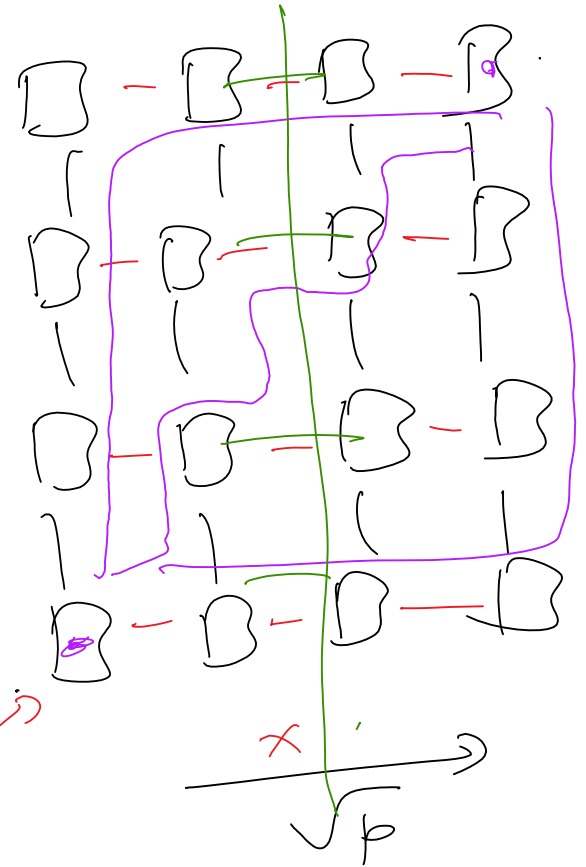
Bussec. band.

✓  $\sqrt{p}$

# links per node = 4



// square mesh.



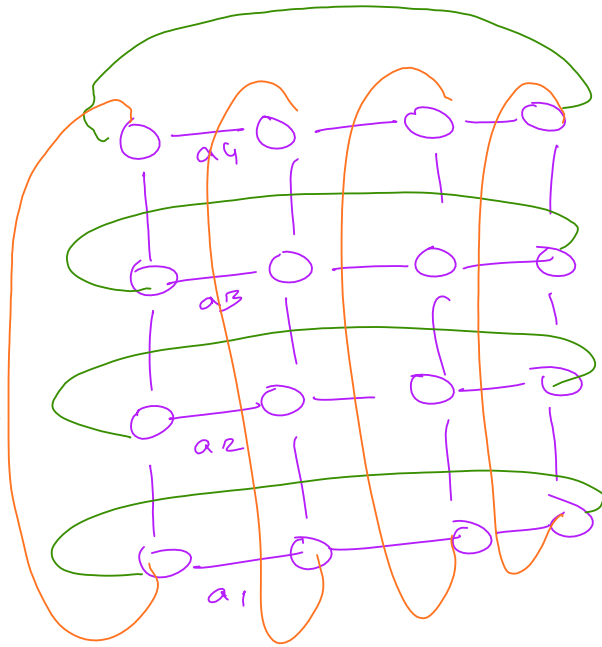
# Torus

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TORUS

⇒ A wrap-around mesh

2D torus ⇒



The IBM Blue Gene/Q supercomputer is an example in realworld which has a 5-D Torus.

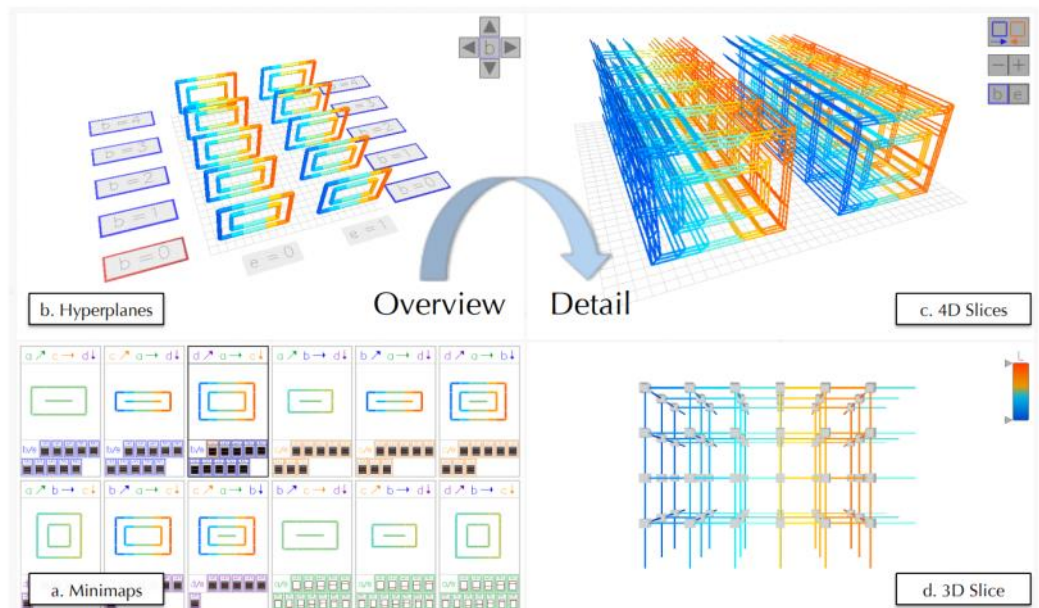


Fig. 1: Visualization of IBM Blue Gene/Q Five-dimensional torus interconnection network using four linked views.

Picture courtesy of:

McCarthy, Collin M., Katherine E. Isaacs, Abhinav Bhatele, Peer-Timo Bremer, and Bernd Hamann. "Visualizing the five-dimensional torus network of the IBM Blue Gene/Q." In *Proceedings of the First Workshop on Visual Performance Analysis*, pp. 24-27. IEEE Press, 2014.

# Hypercube

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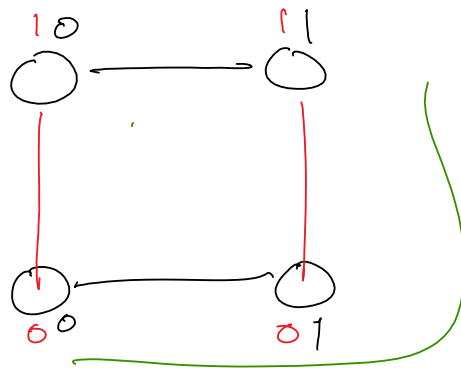
4) Hypercube Topology: (p: processors)  $\Rightarrow 2^d$  nodes

Let  $d$ : # dimensions.

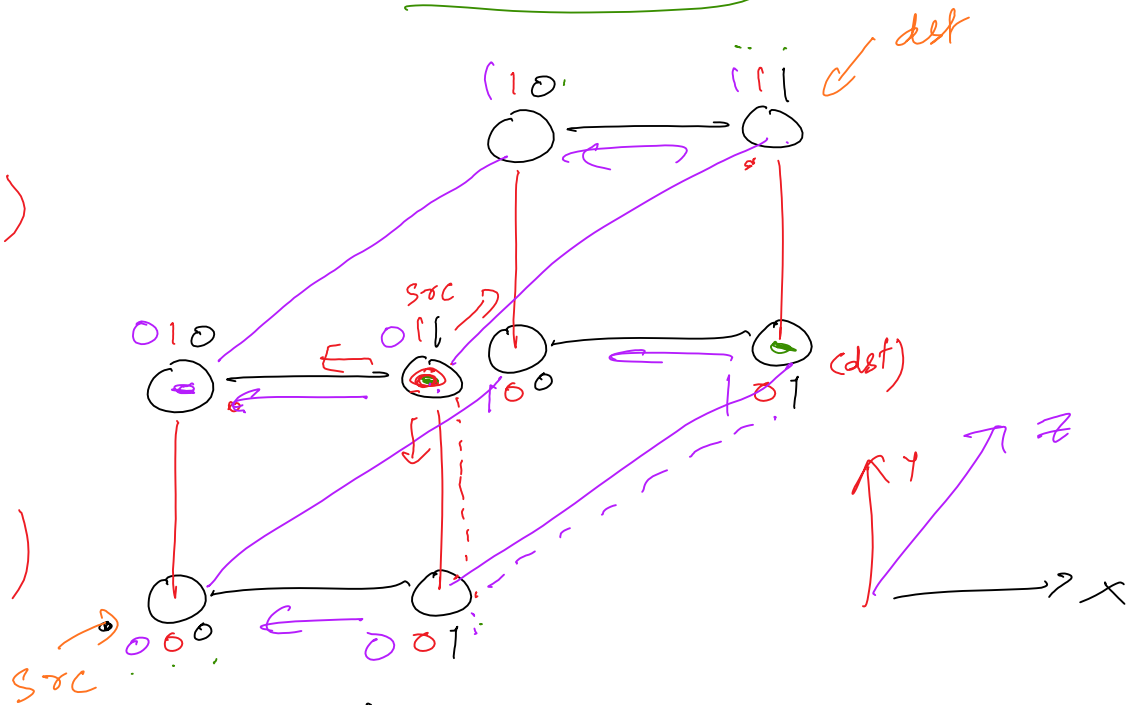
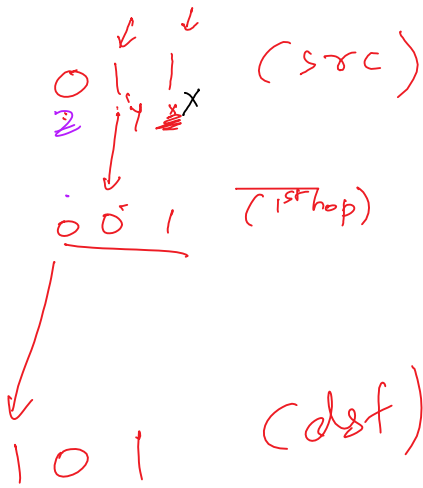
$d=1$



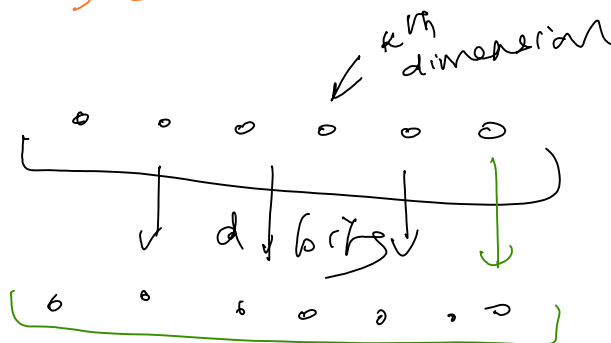
$d=2$



$d=3$



process rank:  
(src)  $\downarrow$   
(dst)

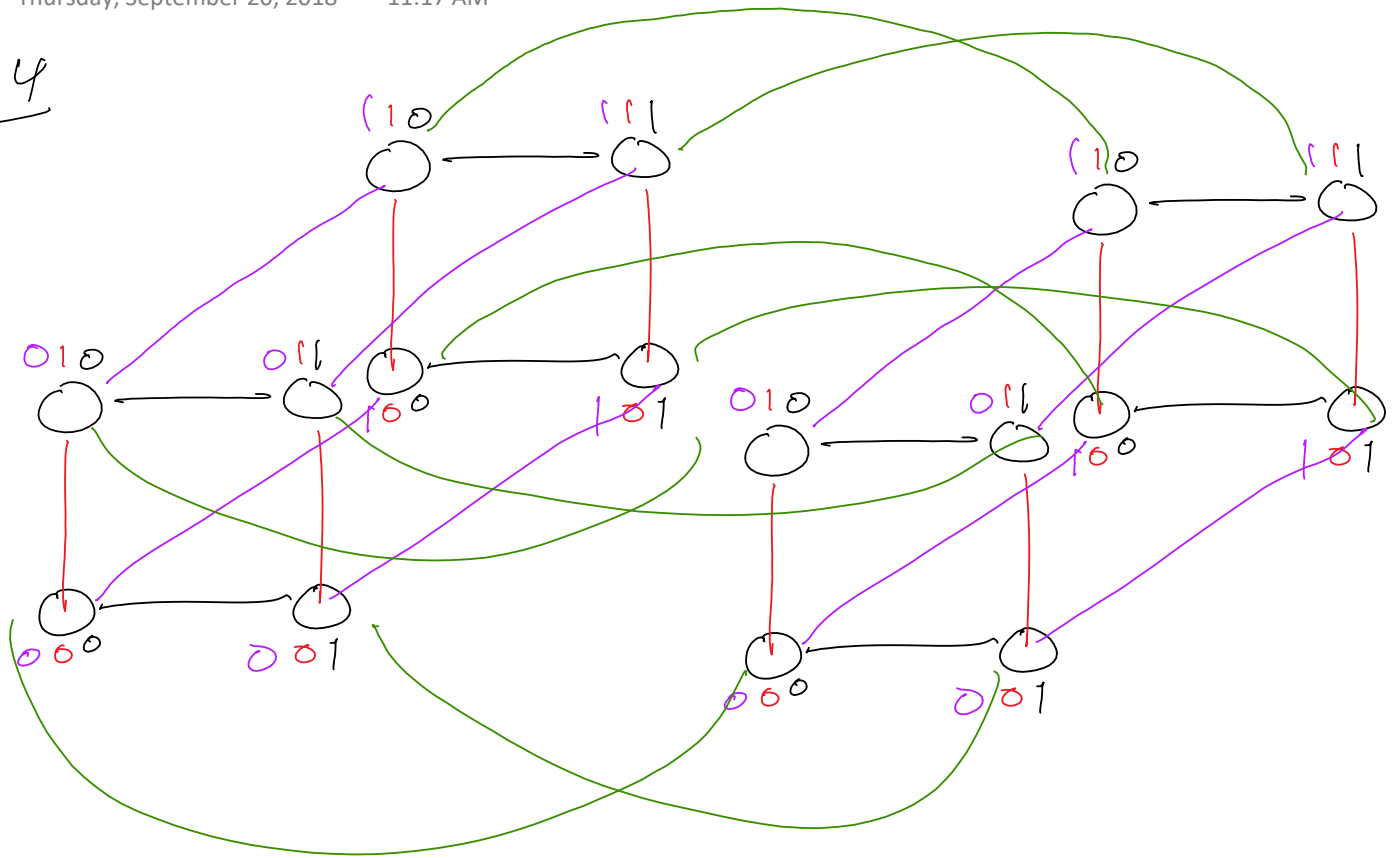


How many procs  
 $= 2^d$

# Hypercube:

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$d=4$



Basic prop:

- 1) #procs ( $p$ ) =  $2^d = 2^{d-1} + 2^{d-1}$
- 2) Diameter =  $d = \lg_2 p$  ✓
- 3) Links per node =  $d = \lg p$  ✗
- 4) BiSec. B/W =  $2^{d-1} = \frac{1}{2} p$  ✓

$LPN = \min \{ C, \lg p \}$   
 (real world)  
 ↗  
 4 or 5

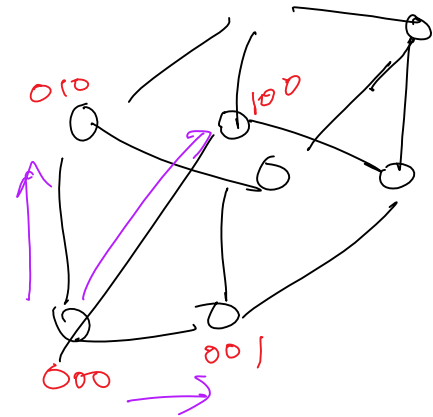
# Hypercubic permutation

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Example where a hypercube permutation could help write "good" parallel programs;

E.g. Reduce (operator)

$i \leftarrow$  my proc. rank  
 $p \leftarrow$  # procs.



Reduce ( )

Init local-result

for ( $t = 0$  to  $(\lg p - 1)$ )

$j \leftarrow$  toggle the  $t^{\text{th}}$  least significant bit in the binary representation of  $i$

communicate with proc. rank  $j$

Example:

