

Parallel Random Number

Tuesday, October 16, 2018 11:20 AM

Detailed Parallel Algorithm:

step 1) - load input parameters $\{x_0, A, B, P, n\}$ on all procs.

Step 2) At each process P_j .

a) Initialize: Matrix $M = \begin{bmatrix} A & 0 \\ B & I \end{bmatrix}$, $M^0 = \begin{bmatrix} 1 & 0 \\ 0 & 1 \end{bmatrix}$

b) Initialize: - Array X_{local} of size $\frac{n}{p}$, with each element of type a 2×2 Matrix.

- Init: $X_{local} = \begin{bmatrix} 0 & & & & \\ M & M & \dots & & M \end{bmatrix}$ $\frac{n}{p} \times \frac{n}{p}$

Step 3) At each process P_j :

• $M_{local} = M^0$

• for ($i = 0$ to $\frac{n}{p} - 1$)

$M_{local} = M_{local} \otimes X_{local}^{[i]}$

Parallel Random Number

Tuesday, October 16, 2018 11:20 AM

Step 4) Run p -element parallel Prefix, with each process providing its correspond M_{local} as input, and \otimes as the matrix multiplication operator.

• Output will be a 2×2 matrix, say M_{off} which represents the prefix matrix product.

M_{off} at process p_j
will be equal to: $M_{j \frac{n}{p}}$

Step 5) At every process p_j :

- call serial-matrix $\left(\frac{n}{p}\right)$, with two modifications:

- Initialize its $M_{\text{next}} \leftarrow M_{\text{off}}$
- Run its for loop from 0 to $n-1$

Output X from every process.