# A Passivity Control Strategy for VSC-HVDC Connected Large Scale Wind Power

Xinming Fan, Lin Guan, Chengjun Xia, Jianming He

Abstract--For wind farm connection VSC-HVDC transmission has obvious technical and economic advantages, but concentrated integration of large scale wind power requires stronger robustness. Based on the mathematical model of VSC-HVDC in abc frame, the Euler-Lagrange mathematical model of voltagesource-converter(VSC) in d-q rotating frame is built and the strict passivity of VSC is proved. Based on the energy dissipativity of VSC, energy storage function is established by using state error and it is used as Lyapunov function, VSC-HVDC is astringed to expected stable equilibrium point rapidly by damping addition. The passivity controller is designed according to expected equilibrium point, state variable and state error, and decoupling control for various variable is achieved. With different operation conditions, VSC-HVDC and its control system are simulated by software PSCAD/EMTDC, the results show that the proposed control strategy has good performance and strong robustness either in dynamic state or steady state.

Index Terms--large scale wind power, VSC-HVDC, passivity, EL mathematical model, error storage function, decoupling control.

#### I. INTRODUCTION

Wind power is the main alternative energy when every country fulfils its renewable energy development goals. By the end of 2010, 196630MW wind power has been installed all over the world[1]. Meanwhile large scale wind farms of hundreds of MWs of power are developed in many countries around the world. With the development of wind turbine and power electronics technologies, wind farms are being changed from small-sized, distributed and locallyconnected to large-scale, highly concentrated and remote high voltage transmission[2][3]. HVDC with voltage source converter (VSC-HVDC) has fine dynamic characteristic and transmission flexibility, furthermore, it improves the stability of power system [4]-[7]. In addition, in comparison with other solutions VSC-HVDC is more economical for hundred megawatts wind farm[8][9]. Therefore, VSC-HVDC has obvious technical and economic advantages for the connection of large scale wind farm.

The VSC-HVDC system can be operated in three modes: 1) constant DC voltage control mode; 2) constant active and reactive power control mode; and 3) constant AC voltage control mode[10]. Therefore the control of DC/AC voltage and power is very important, especially at least one of the converter stations has to control the DC voltage to make the active power balanced and the DC voltage stable[11][12]. However four control inputs of the VSC-HVDC transmission link and their interaction makes the system a truly nonlinear multiple-input multiple-output control system. Voltage vector oriented double closed-loop PID control based on synchronous rotating reference frame is the most common method to solve the nonlinear problem [13] [14]. Moreover, some advanced control strategies are applied to VSC-HVDC transmission link that include feedback linearization and sliding mode control to achieve decoupled control of multiple-input multiple-output variable[10], adaptive control based on backstepping method to improve the dynamic characteristic of VSC-HVDC[15], fuzzy-PI inner loop control applied to voltage source converter[16], and PID neural network sliding mode controller for voltage source converter[17]. But it is difficult to achieve ideal effects because of the multivariable structure and highly coupled nonlinearity of the VSC-HVDC system.

Passivity control is an emerging nonlinear control theory based on the energy dissipation of system[18][19], and was applied to many areas successfully [20][21]. In this paper the passivity controller of VSC is deisigned based on Eulerlagrange(EL) mathematical mode of VSC-HVDC. The control strategy makes the VSC-HVDC transmission linked large scale wind farm has better static and dynamic performance and stronger robustness. The simulation results under different operation conditions show its superiority.

## II. TOPOLOGY AND MATHEMATICAL MODEL OF THE VSC-HVDC TRANSMISSION SYSTEM

The single line diagram of the VSC-HVDC transmission connected a wind farm is shown in Fig.1. Wind farm is connected to the sending end VSC by a transformer, the receiving end VSC is linked to the main network, and both VSC connected to each other by long distance DC transmission line. The detailed structure of VSC is shown in Fig.2, the transformer reactance and power loss are equivalent to L and R, and the parameters of the three phase circuits are assumes to be identical. *Usa*, *Usb* and *Usc* are phase voltage at

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the point of common coupling (PCC),  $i_a$ ,  $i_b$  and  $i_c$  are line current at PCC.  $u_a$ ,  $u_b$  and  $u_c$  are phase voltage at the AC side of the converter,  $u_{dc}$  is the dc voltage,  $i_{dc}$  is DC current in the DC transmission line.



Fig.2 VSC-HVDC circuit topology

The mathematical model of the VSC-HVDC VSC in the three phase static frame is

$$\begin{cases} L\frac{dia}{dt} = u_{sa} - u_a - Ri_a = u_{sa} - u_{dc}(s_a - \frac{1}{3}\sum_{j=a,b,c}s_j) - Ri_a\\ L\frac{dib}{dt} = u_{sb} - u_b - Ri_b = u_{sb} - u_{dc}(s_b - \frac{1}{3}\sum_{j=a,b,c}s_j) - Ri_b\\ L\frac{dic}{dt} = u_{sc} - u_c - Ri_c = u_{sc} - u_{dc}(s_c - \frac{1}{3}\sum_{j=a,b,c}s_j) - Ri_c\\ c\frac{du_{dc}}{dt} = s_ai_a + s_bi_b + s_ci_c - i_dc \end{cases}$$
(1)

Where  $S_j$  (j=a,b,c) is the logic switch function, when  $S_j = 1$  the upper bridge arm is conductive and lower bridge arm is turn-off, when  $S_j = 0$  the contrary is the case. By Park transformation matrix and its inverse matrix, equation (1) can be transformed to mathematical model in d-q synchronous rotating frame as equation (2)

$$\begin{cases} L\frac{di_d}{dt} = u_{sd} - u_d - Ri_d - \omega Li_q = u_{sd} - s_d u_{dc} - Ri_d - \omega Li_q \\ L\frac{di_q}{dt} = u_{sq} - u_q - Ri_q + \omega Li_d = u_{sq} - s_q u_{dc} - Ri_q + \omega Li_d \end{cases}$$
(2)  
$$\frac{2}{3}c\frac{du_{dc}}{dt} = s_{did} + s_q i_q - \frac{2}{3}i_{dc}$$

Where Sd and Sq represent the d and q components of the switch function,  $u_{sd}$  and  $u_{sq}$  are the d and q components of the voltage at PCC, ud and uq are the d and q components of the voltage at AC side of the converter. The active power  $p_s$  and reactive power  $q_s$  in the d-q synchronous rotating coordinates are

$$p_{s} = \frac{3}{2} (u_{sd}i_{d} + u_{sq}i_{q})$$

$$q_{s} = \frac{3}{2} (u_{sd}i_{q} - u_{sq}i_{d})$$
(3)

When d axis is oriented at the vector of the voltage at PCC, then  $u_{sq} = 0$ , and  $p_s = \frac{3}{2}u_{sd}i_d$ ,  $q_s = \frac{3}{2}u_{sd}i_q$ , so controlling the  $i_d$  and  $i_q$  respectively can realize the decoupled control of  $p_s$  and  $q_s$ .

## III. EL MODEL OF VSC-HVDC CONVERTER

Transform the equation (2) to the form of (4)

$$\begin{bmatrix} L & 0 & 0 \\ 0 & L & 0 \\ 0 & 0 & \frac{2}{3}C \end{bmatrix} \begin{bmatrix} \frac{dId}{dt} \\ \frac{di_q}{dt} \\ \frac{dU_{dc}}{dt} \end{bmatrix} + \begin{bmatrix} R & 0 & 0 \\ 0 & R & 0 \\ 0 & 0 & 2/3R_{dc} \end{bmatrix} \begin{bmatrix} i_d \\ i_q \\ u_{dc} \end{bmatrix} + \begin{bmatrix} 0 & \omega L & s_d \\ -\omega L & 0 & s_q \\ -s_d & -s_q & 0 \end{bmatrix} \begin{bmatrix} i_d \\ i_q \\ u_{dc} \end{bmatrix} = \begin{bmatrix} u_{sd} \\ u_{sg} \\ 0 \end{bmatrix}$$
(4)

Where  $R_{dc} = u_{dc} / i_{dc}$  is the equivalent resistance at the DC side of the converter. According to the Euler-lagrange Equation[22][20], Equation (4) has the form

$$M\dot{x} + \Re x + Jx = u \tag{5}$$

Where *M* is the positive definite diagonal matrix;  $\Re$  is the positive definite matrix and characterizes the passivity; *J* is antisymmetric matrix,  $J = -J^{T}$ , and reflects the interconnection character of state variable; *u* is the control inputs. According to equation (4), the detailed expressions of above matrixes are

$$M = \begin{bmatrix} L & 0 & 0 \\ 0 & L & 0 \\ 0 & 0 & \frac{2}{3}C \end{bmatrix}, \ \mathfrak{R} = \begin{bmatrix} R & 0 & 0 \\ 0 & R & 0 \\ 0 & 0 & 2/(3Rdc) \end{bmatrix},$$
$$J = \begin{bmatrix} 0 & \omega L & sd \\ -\omega L & 0 & sq \\ -sd & -sq & 0 \end{bmatrix}, \ x = \begin{bmatrix} x_1 \\ x_2 \\ x_3 \end{bmatrix} = \begin{bmatrix} id \\ iq \\ udc \end{bmatrix}, \ u = \begin{bmatrix} usd \\ usg \\ 0 \end{bmatrix}.$$

Assuming that the energy storage function of voltage source converter is  $H = \frac{1}{2}x^{T}Mx$ , then deducing by equation (5) may get

 $\dot{H} = x^{\mathrm{T}}M\dot{x} = x^{\mathrm{T}}(u - Jx - \Re x) = x^{\mathrm{T}}u - x^{\mathrm{T}}\Re x$  (6) Now makes the output y = x, the energy supply rate  $s(u, y) = u^{\mathrm{T}}y$ , positive definite function is  $Q(x) = x^{\mathrm{T}}\Re x$ , then the energy storage of the system is

$$H[x(t)] - H[x(0)] \le \int_0^t u^{\mathrm{T}} y d\tau - \int_0^t x^{\mathrm{T}} \Re x d\tau \qquad (7)$$

 $\dot{H} \leq u^{\mathrm{T}} y - Q(x)$ 

(8)

or

Consequently, the VSC is strictly passive. The attenuation characteristics of energy function just reflects stability of Lyapunov and energy function is exactly used as Lyapunov function.

## IV. PASSIVITY CONTROLLER DESIGNED FOR CONVERTER

When VSC-HVDC converter is at steady state, the variables of expected stable equilibrium points  $x_1^* = id^*$ ,  $x_2^* = iq^*$ ,  $x_3^* = udc^*$ . The error storage function is choosed as  $H_e = \frac{1}{2} x_e^T M x_e$ , and  $x_e = x - x^*$ , from equation (5) we obtain

$$M\dot{x}_{e} + \Re x_{e} + Jx_{e} = u - (M\dot{x}^{*} + \Re x^{*} + Jx^{*})$$
(9)

To make the error storage function equal to zero and the system astringe to expected equilibrium point quickly, the energy dissipation should be accelerated and damping is added. The damping is

$$\mathfrak{R}_{d} = (\mathfrak{R} + \mathfrak{R}_{a}) \tag{10}$$

Where  $\Re_a$  is positive definite matrix, then equation (9) is transformed to

$$M\dot{x}_e + \Re_d x_e + Jx_e \tag{11}$$

$$= u - (M\dot{x}^* + \Re x^* + Jx^*) + \Re_a x_e$$

Make the equation

$$u - (M\dot{x}^* + \Re x^* + Jx_e + Jx^*) + \Re a x_e = 0$$
 (12)

And  $M\dot{x}_e + \Re_d x_e = 0$ , then

$$\dot{H}_e = x_e^{\mathrm{T}} M \dot{x}_e = -x_e^{\mathrm{T}} \Re_{\mathrm{d}} x_e < 0$$
 (13)

Equation (13) shows the error storage function can astringe quickly and its convergence rate is influenced by  $\Re_a$ . According to equation (12), gets the passivity control law and it is

$$s_{dUdc} = u_{sd} + R_{a}i_{d} - (R + R_{a})i_{d}^{*} - \omega Li_{q}$$

$$s_{q}u_{dc} = u_{sq} + R_{a}i_{q} - (R + R_{a})i_{q}^{*} + \omega Li_{d}$$
(14)

Equation (14) could be written in

$$u_{d} = u_{sd} + R_{a}i_{d} - (R + R_{a})i_{d}^{*} - \omega Li_{q}$$

$$u_{q} = u_{sq} + R_{a}i_{q} - (R + R_{a})i_{q}^{*} + \omega Li_{d}$$
(15)

Therefore the voltage at the AC side of converter can be get from equation (15). Substituting equation (14) in equation (2) gets

$$\begin{cases} L \frac{di_d}{dt} = (R + R_a)(i_a^* - i_d) \\ L \frac{di_q}{dt} = (R + R_a)(i_q^* - i_q) \\ c \frac{du_{dc}}{dt} = (u_{dc}^* - u_{dc}) / R_{dc} + 3R_a(u_{dc}^* - u_{dc}) / 2 \end{cases}$$
(16)

Equation (16) shows  $i_d$ ,  $i_q$  and  $\mathcal{U}_{dc}$  can be stable at expected equilibrium points when  $\Re_a$  is big enough. In addition, it shows the control law can achieve decoupled control for  $i_d$ ,  $i_q$  and  $\mathcal{U}_{dc}$ .  $i_d^*$  and  $i_q^*$  can be got from the outer control loop. In order to facilitate active power setting and voltage control for wind farm, active power and constant voltage control are used at the sending end, Fig.3 shows the control diagram.





To meet active power balance and DC voltage stability, constant DC voltage and constant AC voltage controls are used at receiving end, Fig.4 shows the control diagram.



Fig.4 Passivity decoupled control strategy for receiving-end VSC

#### V. SIMULATION AND ANALYSIS

In order to verify the validity and superiority of the proposed control stratey, the VSC-HVDC transmission linked wind farm and its control strategy are modeled and simulated by software PSCAD/EMTDC. The rated DC voltage of the VSC-HVDC link is  $\pm 160$ kV, the converter capacity is 200MVA and the base capacity is 100MVA. The power production of the wind farm is 180MW, the PCC voltage of both ends is 110kV and the damping resistor  $R_a = 0.6$ pu .The simulation time span is 20s. Comparison is made with PI double closed-loop control and passivity control, and the outer-loop PI control parameters of both are identical so as to ensure comparative anslysis valid. Fig.5 to Fig.8 shows the steady simulation results.



(a) Generated power and transmited power under PI double closed-loop control





Simulation resluts in Fig.5(b), Fig.6(b), Fig.7 and Fig8(b) show that AC voltage, wind power production, active power transmitted, DC voltage and DC current reach set value quickly and keep stable, no oscillation and very small overshoot under passivity control. Comparsion with PI control demonstrate that passivity control make the system have stronger robustness.

In order to compare dynamic response performances, make the wind speed have a step change at 10s and 15s under both control mode, as shown in Fig.9, and Fig.10 to Fig.13 show the simulation results of each variable.



(b) Generated power and transmited power under passivity control Fig.11 Generated power and transmited power under step wind disturbance



The simulation resluts show that the AC voltage at both ends PCC have a little fluctuation change and reach stability quickly when wind speed step up or down under both control stragtegies, as shown in Fig.10. The power transmitted by VSC-HVDC is consistent with the wind power production which changes with wind speed changes, and the transmission link remains stable even if power changes with ±60MW, as shown in Fig.11. Fig12(a) shows the DC voltage at sending end changes with wind speed changes, but the fluctuation is little and flutter is smaller under passivity control. The receiving end DC voltage is stabilized on set value and error is  $\pm 0.05$ kV under passivity control, but it fluctuates greatly and need much time to reach stability under PI double closed-loop control, as shown in Fig.12(b). In addition, the DC current changes with transmitted power changes, but its ripple is little under passivity control, as shown in Fig.13.

Setting the voltage amplitude step change at the coupling

point of receiving end to simulate voltage disturbance of connected grid, as shown in Fig.14. Fig.15 and Fig.16 shows the results.





Fig.16 DC voltage of receiving end under step voltage disturbance at asscess point of receiving end

The AC voltage at both ends is stabilized on expected value and disturbance is admissible when the voltage at access point change, but it has little ripple and better steady performance under passivity control, as shown in Fig15. As to DC voltage at receiving end, its static error is smaller, recover to set value with quick dynamic response after disturbance under passivity control, as shown in Fig.16.

## VI. CONCLUSION

VSC-HVDC transmission link is a significant scheme to connect large scale wind power. Aiming at the problem of robustness existed in the VSC-HVDC transmission link, a passivity control strategy is proposed for converter in this paper. Error energy storage function is established and used as Lyapunov function based on the EL mathematical model of converter in d-q rotating coordinates. Based on damping addition, expected equilibrium point, state variable and state error, passivity controller is designed, and decoupled control for every variable is achieved. The proposed model and control strategy are siumulated by software PSCAD/EMTDC, and the results shows the control system has good static and dynamic performance and robustness.

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