## **Homework Assignment 1** (Due 4:10pm, Jan. 25)

**[Transistor Characteristics]** Assume that  $V_{tn} \approx V_{DD}/4$ .



(1) [10 points] Draw a graph of  $V_D$  (x-axis) vs.  $V_S$  (y-axis) for  $V_G = 0$ .



If  $V_G$  is 0V, the NFET is always turned off, so  $V_S$  holds the initial value.

(2) [10 points] Draw a graph of  $V_D$  (x-axis) vs.  $V_S$  (y-axis) for  $V_G = V_{DD}$ .



If  $V_G = V_{DD}$ , the NFET is turned on only when  $V_S \leq V_{DD} - V_{tn}$  is satisfied. When the NFET is turned on, the drain and the source terminals are connected, so  $V_S = V_D$ .

(3) [10 points] Draw a graph of  $V_G$  (x-axis) vs.  $V_S$  (y-axis) for  $V_D = 0$ .



Assume  $V_S = 0$  V. If  $V_G < V_{tn}$ , the NFET is turned off, so  $V_S$  is 0V. If  $V_G > V_{tn}$ , the NET is turned on, but  $V_D = 0$ , so  $V_S$  is always 0V.

(If  $V_S$  was a certain value, it holds the value if  $V_G < V_{tn}$ . If  $V_G$  is greater than  $V_{tn}$ , however, the NFET is turned on and the charges stored in the capacitor will be discharged, so  $V_S$  will be 0V).

(4) [10 points] Draw a graph of  $V_G$  (x-axis) vs.  $V_S$  (y-axis) for  $V_D = V_{DD}$ .



Assume  $V_S = 0$  V. If  $V_G < V_{tn}$ , the NFET is turned off, so  $V_S = 0$  V. If  $V_G > V_{tn}$ , the NFET is turned on and the capacitor will be charged. However, the NFET is turned off if  $V_{GS} < V_{tn}$ , i.e.,  $V_S > V_G - V_{tn}$ .

**[Transistor Characteristics]** Assume that  $|V_{tp}| \approx V_{DD}/4$ .



(5) [10 points] Draw a graph of  $V_S$  (x-axis) vs.  $V_D$  (y-axis) for  $V_G = 0$ .



The PFET is ON if  $V_{SG} > |V_{tp}|$ . Since  $V_G = 0V$ , the PFET is ON if  $V_S > |V_{tp}|$ .

(6) [10 points] Draw a graph of  $V_S$  (x-axis) vs.  $V_D$  (y-axis) for  $V_G = V_{DD}$ .



 $V_{SG}$  is always less than or equal to 0V in this case, so the PFET is always OFF. Thus,  $V_D$  holds the initial value.

(7) [10 points] Draw a graph of  $V_G$  (x-axis) vs.  $V_D$  (y-axis) for  $V_S = 0$ .



Assume  $V_D = 0$ V. Then,  $V_{SG} = 0 - V_G \le 0$ V, so the PFET is always OFF. In this case,  $V_D$  holds its initial value.

(8) [10 points] Draw a graph of  $V_G$  (x-axis) vs.  $V_D$  (y-axis) for  $V_S = V_{DD}$ .



The PFET is ON if  $V_{SG} = V_{DD} - V_G > |V_{tp}|$ , i.e., if  $V_G < V_{DD} - |V_{tp}|$ . In this case,  $V_D$  will be  $V_{DD}$ . If  $V_G > V_{DD} - |V_{tp}|$ , the PFET is turned off and the  $V_D$  will hold the last value, which is  $V_{DD}$ .

(9) [10 points] Design the following logic using NFETs and PFETs. Available inputs: A, B, C. Try to minimize # TRs.

$$F = A \cdot (\overline{B + C})$$
$$F = A \cdot (\overline{B + C}) = \overline{\overline{F}} = \overline{\overline{A} + B + C}$$

