

**EE434**

**ASIC and Digital Systems**

**Final Exam**

**May 5, 2020. (8am – 10am)**

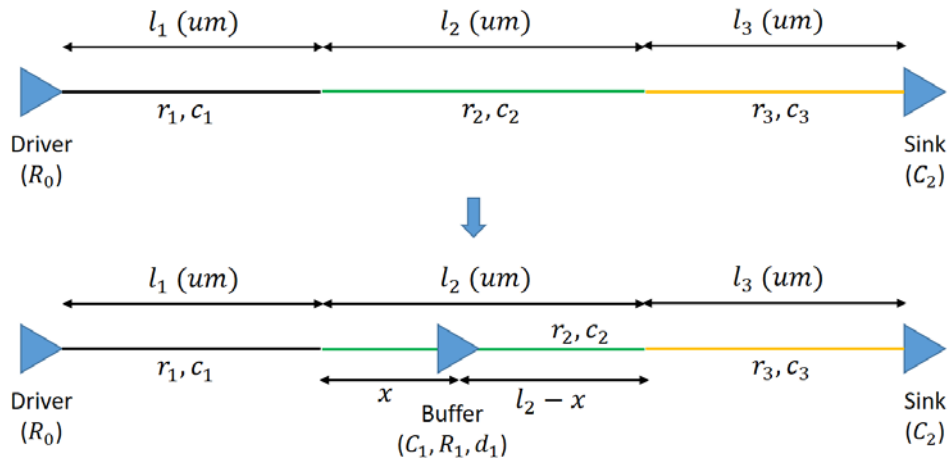
**Instructor: Dae Hyun Kim ([daehyun@eecs.wsu.edu](mailto:daehyun@eecs.wsu.edu))**

**Name:**

**WSU ID:**

Problem	Points	
1	30	
2	40	
3	30	
4	50	
5	20	
6	50	
7	40	
Total	260	

## Problem #1 (Interconnects, 30 points)



The figure shows a net composed of three wire segments. The length and unit wire  $R$  and  $C$  of section  $k$  ( $k = 1, 2, 3$ ) are  $l_k$ ,  $r_k$ , and  $c_k$ , respectively as shown in the figure. The output resistance of the driver is  $R_0$ , the input capacitance of the sink is  $C_2$ , and the output resistance, input capacitance, and the delay of a buffer is  $R_1$ ,  $C_1$ , and  $d_1$ , respectively. We are going to insert a buffer into the second section ( $0 \leq x \leq l_2$ ). The first and third sections are not bufferable.

(a) Find the optimal location for the buffer insertion (express  $x$  as a function of the constants). (10 points)

(b) Answer the following questions. (Correct: +2 points. Wrong: -1 point. No answer: 0.)

(1) If  $R_0 = R_1$ ,  $C_1 = C_2$ ,  $r_1 = r_2 = r_3$ ,  $c_1 = c_2 = c_3$ , and  $l_1 = l_2 = l_3$ , then  $x = \frac{1}{2}l_2$ . (True / False)

(2) If  $R_0 < R_1$ ,  $C_1 = C_2$ ,  $r_1 = r_2 = r_3$ ,  $c_1 = c_2 = c_3$ , and  $l_1 = l_2 = l_3$ , then  $x < \frac{1}{2}l_2$ . (True / False)

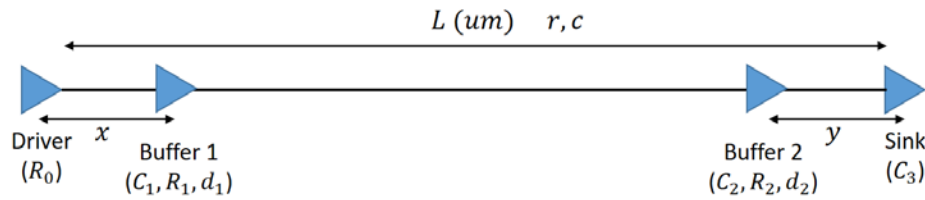
(3) If  $R_0 = R_1$ ,  $C_1 < C_2$ ,  $r_1 = r_2 = r_3$ ,  $c_1 = c_2 = c_3$ , and  $l_1 = l_2 = l_3$ , then  $x < \frac{1}{2}l_2$ . (True / False)

(4) If  $R_0 = R_1$ ,  $C_1 = C_2$ ,  $r_1 < r_2 = r_3$ ,  $c_1 = c_2 = c_3$ , and  $l_1 = l_2 = l_3$ , then  $x < \frac{1}{2}l_2$ . (True / False)

(5) If  $R_0 = R_1$ ,  $C_1 = C_2$ ,  $r_1 = r_2 > r_3$ ,  $c_1 = c_2 = c_3$ , and  $l_1 = l_2 = l_3$ , then  $x < \frac{1}{2}l_2$ . (True / False)

- (6) If  $R_0 = R_1$ ,  $C_1 = C_2$ ,  $r_1 = r_2 = r_3$ ,  $c_1 < c_2 = c_3$ , and  $l_1 = l_2 = l_3$ , then  $x < \frac{1}{2}l_2$ . (True / False)
- (7) If  $R_0 = R_1$ ,  $C_1 = C_2$ ,  $r_1 = r_2 = r_3$ ,  $c_1 = c_2 > c_3$ , and  $l_1 = l_2 = l_3$ , then  $x < \frac{1}{2}l_2$ . (True / False)
- (8) If  $R_0 = R_1$ ,  $C_1 = C_2$ ,  $r_1 = r_2 = r_3$ ,  $c_1 = c_2 = c_3$ , and  $l_1 < l_2 = l_3$ , then  $x < \frac{1}{2}l_2$ . (True / False)
- (9) If  $R_0 = R_1$ ,  $C_1 = C_2$ ,  $r_1 = r_2 = r_3$ ,  $c_1 = c_2 = c_3$ , and  $l_1 = l_2 > l_3$ , then  $x < \frac{1}{2}l_2$ . (True / False)
- (10) If  $r_3$  increases,  $x$  increases (i.e., the optimal buffer location is shifted to the right.) (True / False)

## Problem #2 (Interconnects, 40 points)



The figure shows a net composed of a long wire whose unit resistance and capacitance are  $r$  and  $c$ , respectively. We want to insert two buffers, Buffer 1 and Buffer 2 ( $0 \leq x$ ,  $0 \leq y$ ,  $x + y \leq L$ ). The output resistance ( $R_{\#}$ ), input capacitance ( $C_{\#}$ ), and internal delay ( $d_{\#}$ ) of each cell are shown above.

(a) Find the optimal locations for Buffer 1 and Buffer 2 (express  $x$  (and also  $y$ ) as a function of the constants). Hint: Express the total delay as a function of  $x$  and  $y$ . Then, differentiate it w.r.t.  $x$  and set it to zero. Differentiate it w.r.t.  $y$  and set it to zero. Then, you get two equations for two variables,  $x$  and  $y$ . Solve it. (12 points)

$x =$

$y =$

(b) Answer the following questions. (Correct: +2 points. Wrong: -1 point. No answer: 0.)

Notice that if  $x$  increases, Buffer 1 is shifted to the right.

However, if  $y$  increases, Buffer 2 is shifted to the left.

(1) If  $R_0 = R_1 = R_2$  and  $C_1 = C_2 = C_3$ , then  $x = \frac{1}{3}L$ . (True / False)

(2) If  $R_0 = R_1 = R_2$  and  $C_1 = C_2 = C_3$ , then  $y = \frac{1}{3}L$ . (True / False)

(3) If  $R_0$  increases,  $x$  increases. (True / False)

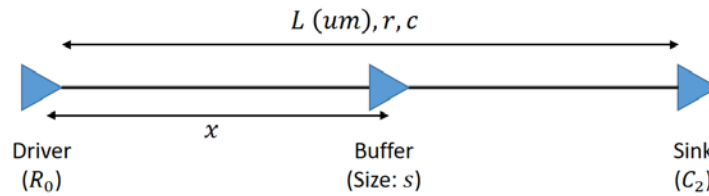
(4) If  $R_0$  increases,  $y$  increases. (True / False)

(5) If  $R_1$  increases,  $x$  increases. (True / False)

(6) If  $R_1$  increases,  $y$  increases. (True / False)

- (7) If  $R_2$  increases,  $x$  increases. (True / False)
- (8) If  $R_2$  increases,  $y$  increases. (True / False)
- (9) If  $C_1$  increases,  $x$  increases. (True / False)
- (10) If  $C_1$  increases,  $y$  increases. (True / False)
- (11) If  $C_2$  increases,  $x$  increases. (True / False)
- (12) If  $C_2$  increases,  $y$  increases. (True / False)
- (13) If  $C_3$  increases,  $x$  increases. (True / False)
- (14) If  $C_3$  increases,  $y$  increases. (True / False)

### Problem #3 (Interconnects, 30 points)



The figure shows a long wire whose length, unit resistance and capacitance are  $L$ ,  $r$ , and  $c$ , respectively. We want to insert a buffer ( $0 \leq x \leq L$ ). The size of the buffer is  $s$  and its output resistance, input capacitance, and internal delay are as follows:

- Output resistance:  $\frac{R}{s}$  (where  $R$  is a constant)
- Input capacitance:  $sP$  (where  $P$  is a constant)
- Internal delay:  $sD$  (where  $D$  is a constant)

Notice that there are two variables,  $x$  and  $s$ .

(a) Express the total delay as a function of the variables and the constants. (7 points)

$\tau =$

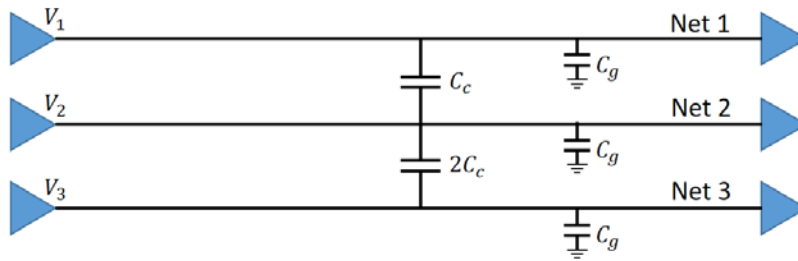
(b) Assuming the location ( $x$ ) is given (i.e., you can treat it as a constant.), find the optimal size ( $s$ ) of the buffer, i.e., express the optimal value of  $s$  as a function of the constants and  $x$ . (7 points)

$s =$

(c) Answer the following questions. (Correct: +2 points. Wrong: -1 point. No answer: 0.)

- (1) If  $x$  increases,  $s$  increases. (True / False)
- (2) If  $R$  increases,  $s$  increases. (True / False)
- (3) If  $c$  increases,  $s$  increases. (True / False)
- (4) If  $C_2$  increases,  $s$  increases. (True / False)
- (5) If  $R_0$  increases,  $s$  increases. (True / False)
- (6) If  $r$  increases,  $s$  increases. (True / False)
- (7) If  $P$  increases,  $s$  increases. (True / False)
- (8) If  $D$  increases,  $s$  increases. (True / False)

### Problem #4 (Coupling, 50 points)



The figure shows three parallel nets. The coupling capacitance between Net 1 and Net 2 is  $C_c$ . The coupling capacitance between Net 2 and Net 3 is  $2C_c$ . The following shows a three-bit binary encoding technique for four decimal numbers (0, 1, 2, 3).

Value	Encoding
0	000
1	010
2	101
3	111

(1) Calculate the total effective capacitance of Net 1 for all possible transitions (0→1, 0→2, 0→3, 1→0, 1→2, 1→3, 2→0, 2→1, 2→3, 3→0, 3→1, 3→2) for the encoding technique, i.e., calculate the sum of the effective capacitances of Net 1 for all possible transitions. (10 points)

(2) Repeat it for Net 2. (10 points)

(3) Repeat it for Net 3. (10 points)

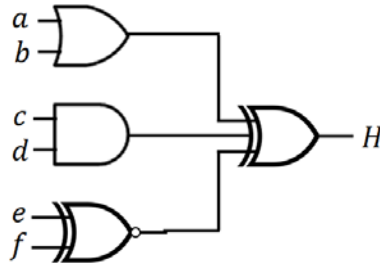
(4) Find a new three-bit encoding of the four values (0, 1, 2, 3) that minimizes the total effective capacitance of the three nets for all possible transitions (Assume  $C_g = C_c$ ). (20 points)

Value	Encoding
0	
1	
2	
3	

Total effective capacitance (for Net 1 + for Net 2 + for Net 3):

### Problem #5 (Testing, 20 points)

The following shows  $H = (a + b) \oplus (c \cdot d) \oplus (\overline{e \oplus f})$ . Answer the following questions.



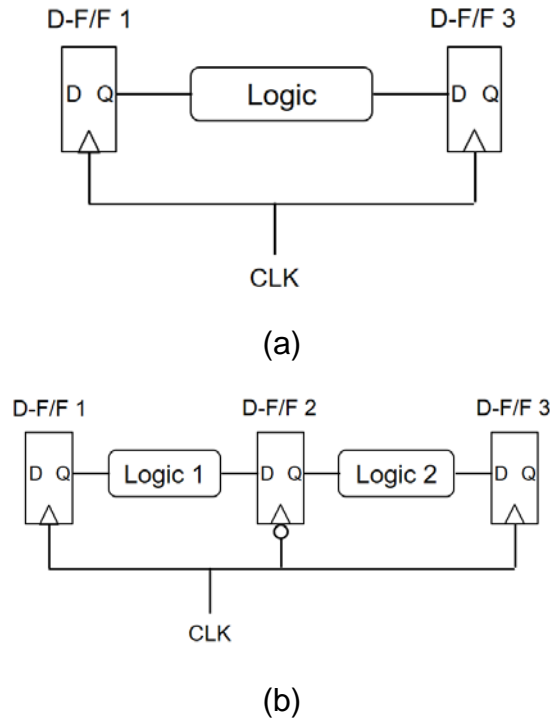
(1) Find all input vectors that can detect a s-a-0 fault at input  $a$ . (10 points)

(2) Find all input vectors that can detect a s-a-1 fault at input  $e$ . (10 points)



## Problem #6 (Static Timing Analysis, 50 points)

The following shows two pipelining methodologies. Figure (a) shows a logic in a single pipeline stage. Figure (b) shows a partitioned version in which two pipeline stages are cascaded and the flip-flop in the middle is negative-edge-triggered.



### Parameters

- $d_1, d_2, d_3$ : The delay from the clock source to Flip-Flop 1, 2, 3
- $c_1, c_2, c_3$ : Clock-to-Q delay ( $T_{CQ}$ ) of Flip-Flop 1, 2, 3
- $s_1, s_2, s_3$ : Setup time of Flip-Flop 1, 2, 3
- $T_A, T_B$ : Clock period for Figure (a) and (b)
- $N (\gg 1)$ : # instructions to execute
- $T_L$ : The logic delay in Figure (a). In Figure (b), the delay of each logic is  $\frac{T_L}{2}$ .
- Execution time of the system in Figure (a):  $(N + 1) \cdot T_A$
- Execution time of the system in Figure (b):  $(N + 3) \cdot T_B$

For the clock periods, we use the minimum clock periods that satisfy all the setup time constraints. Notice that the clock duty cycle is 50%.

(1) The system in Figure (a) has one setup time constraint. Show the inequality. (10 points)

Answer:  $\leq T_A$

(2) The system in Figure (b) has two setup time constraints. Show the inequalities. (16 points)

Answer: 
$$\leq \frac{T_B}{2}$$
$$\leq \frac{T_B}{2}$$

You can merge these two inequalities by just adding them.

$$\leq T_B$$

Use the left term for the next problems.

(3) Now, you have execution times for Figure (a) and (b). Answer the following questions. (24 points)

(a) For Figure (a): If  $d_1$  increases, the execution time increases (True / False).

(b) For Figure (a): If  $c_1$  increases, the execution time increases (True / False).

(c) For Figure (a): If  $T_L$  increases, the execution time increases (True / False).

(d) For Figure (a): If  $d_3$  increases, the execution time increases (True / False).

(e) For Figure (a): If  $s_3$  increases, the execution time increases (True / False).

(f) For Figure (b): If  $d_1$  increases, the execution time increases (True / False).

(g) For Figure (b): If  $c_1$  increases, the execution time increases (True / False).

(h) For Figure (b): If  $T_L$  increases, the execution time increases (True / False).

(i) For Figure (b): If  $d_3$  increases, the execution time increases (True / False).

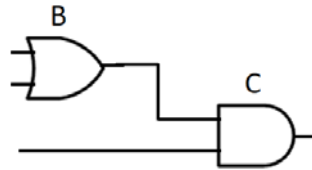
(j) For Figure (b): If  $s_2$  increases, the execution time increases (True / False).

(k) For Figure (b): If  $s_3$  increases, the execution time increases (True / False).

(l) For Figure (b): If  $c_2$  increases, the execution time increases (True / False).

## Problem #7 (Static Timing Analysis, 40 points)

The following shows two gates B and C, which are in the middle of a circuit.



“A gate has a (setup or hold) time violation” means that at least one of the paths going through the gate violates given (setup or hold) time constraints.

(1) Is it possible that gate B has a setup-time violation and gate C has a setup-time violation? Explain why.

(2) Is it possible that gate B has a setup-time violation and gate C has a hold-time violation? Explain why.

(3) Is it possible that gate B has a hold-time violation and gate C has a setup-time violation? Explain why.

(4) Is it possible that gate B has a hold-time violation and gate C has a hold-time violation? Explain why.