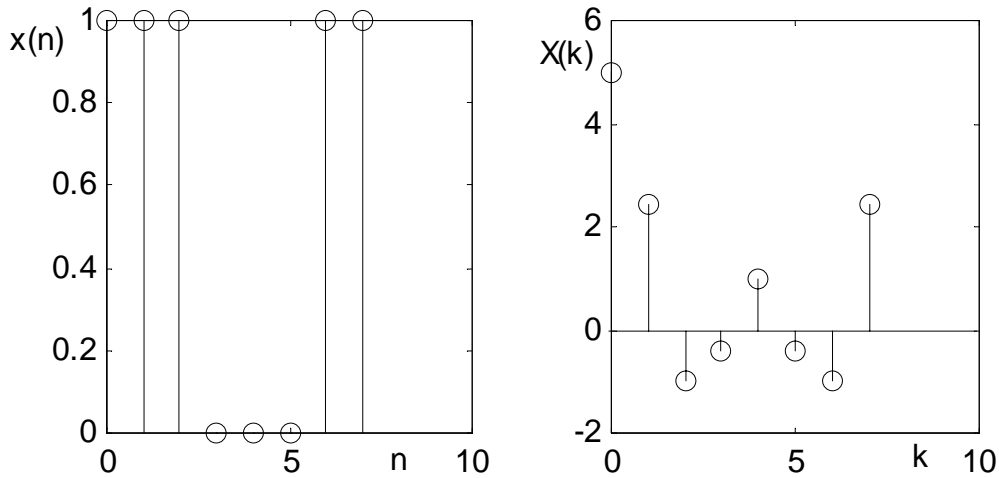


Open book, open notes.

1. Let $h_0(n) = 0.25 [1, 2, 1]$, $h_1(n) = 0.125 [-1, -2, 6, -2, -1]$, $g_0(n) = [0.125 [-1, 2, 6, 2, -1]$, and $g_1(n) = 0.25 [-1, 2, -1]$.

- a. Let $x = [0, 1, 2, 3, 4, 3, 2, 1, 0, 0, 0, \dots]$. Find $y_1(n) = x(n) * h_0(n)$. What is the delay of this filter?
- b. Let $h(n) = h_0(n)*g_0(n) + h_1(n)*g_1(n)$. Find $h(n)$. What is the delay of this filter?

2. Below are plots of $x(n) = [1, 1, 1, 0, 0, 0, 1, 1]$ and its 8-point DFT, $X(k)$.



The signals six signals below are derived from $x(n)$ or $X(k)$. Find, for each case, the correct plot of the respective DFT or IDFT.

- i) $x_1(n) = [x(0), \dots, x(7), x(0), \dots, x(7)]$. Find the plot of the 16-point DFT of $x_1(n)$.
- ii) $x_2(n) = [x(0), 0, x(1), 0, \dots, x(7), 0]$. Find the plot of the 16-point DFT of $x_2(n)$.
- iii) $x_3(n) = (-1)^n x(n)$. Find the plot of the 8-point DFT of $x_3(n)$.
- iv) $x_4(n) = x(n-4)$, (where delay means circular shift). Find the plot of the 8-point DFT of $x_4(n)$.
- v) $x_5(n) = [x(0), \dots, x(7), 0, \dots, 0]$. Find the plot of the 16-point DFT of $x_5(n)$.
- vi) $X_6(k)=[X(0), \dots, X(3), 0.5 X(4), 0, 0, 0, 0, 0, 0, 0.5 X(4), X(5), \dots, X(7)]$. Find the plot of the 16-point IDFT of $X_6(k)$.

Below are twelve figures: the six on the left (a-f) are plots of time signals, the six on the right (h-m) are plots of frequency signals. Correctly match the figures below to the signals to be identified in i) – vi) above.

