

# Learning Greedy Policies for the Easy-First Framework

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## Abstract

Easy-first, a search-based structured prediction approach, has been applied to many NLP tasks including dependency parsing and coreference resolution. This approach employs a learned greedy policy (action scoring function) to make easy decisions first, which constrains the remaining decisions and makes them easier. We formulate greedy policy learning in the Easy-first approach as a novel non-convex optimization problem and solve it via an efficient Majorization Minimization (MM) algorithm. Results on within-document coreference and cross-document joint entity and event coreference tasks demonstrate that the proposed approach achieves statistically significant performance improvement over existing training regimes for Easy-first and is less susceptible to overfitting.

## Introduction

Easy-first is a general search-based structured prediction framework that has been successfully applied to a variety of natural language processing tasks including POS tagging (Shen, Satta, and Joshi 2007), dependency parsing (Goldberg and Elhadad 2010), and coreference resolution (Stoyanov and Eisner 2012; Ratinov and Roth 2012; Hajishirzi et al. 2013). In this framework, the output is constructed incrementally by making the easiest (most confident) decision at each decision step to gather more evidence for making hard decisions later. Consider the following example from the EECB corpus for joint entity and event coreference resolution across documents (Lee et al. 2012).

(a) **A 4.2 magnitude earthquake** struck near a remote area of eastern Sonoma County.

(b) **A tremor** struck Sonoma County.

The coreference resolution decisions for the two verb mentions “struck” and for the two noun mentions containing “Sonoma County” are easy. In contrast, the decision on the two noun mentions “A 4.2 magnitude earthquake” and “A tremor” is hard based on the lexical, syntactic, and semantic constraints or features (Haghighi and Klein 2010; Ng 2010). Once we resolve the coreference of the two verbs and the two “Sonoma County” mentions, we have stronger evidence to help resolve the other two noun mentions.

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The Easy-first approach performs greedy search according to a learned policy (scoring function), which plays a critical role in its effectiveness. The focus of this paper is to study principled ways of learning policies to ensure the success of Easy-first. In particular, we propose a novel online learning algorithm that learns a linear policy for the Easy-first approach. Our contributions are as follows:

- We formulate greedy policy learning as optimizing a non-convex objective consisting of two parts. The first part employs hinge loss to ensure that the learned policy ranks at least one good action higher than all the bad actions. The second part regularizes the weight vector to avoid overly-aggressive updates and over-fitting.
- We develop an efficient majorization-minimization algorithm to optimize the proposed non-convex objective, which iteratively minimizes a convex upper-bound of the objective.
- We evaluate our approach in two NLP domains: within-document entity coreference resolution and cross-document joint entity and event coreference resolution. Our results demonstrate that the proposed approach achieves statistically significant performance improvement over the baseline training approaches for the Easy-first framework and is less prone to overfitting.

## Easy-first Framework and Baseline

This section first formally introduces the Easy-first framework and presents a generic online training procedure. We then describe a popular online learning algorithm for Easy-first, which serves as our baseline.

### Easy-first: inference and training

Given structured inputs  $x \in \mathcal{X}$  and outputs  $y \in \mathcal{Y}$ , we assume a task-specific non-negative loss function  $L$ . The loss function  $L(x, y', y) : \mathcal{X} \times \mathcal{Y} \times \mathcal{Y} \mapsto \mathcal{R}^+$  associates a loss with labeling an input  $x$  with  $y'$  when its true output is  $y$ . There are two key elements in the Easy-first framework: 1) the *search space*  $\mathcal{S}_p$ , whose states correspond to partial structured outputs, and 2) an *action scoring function*  $f$ , which is used to construct the complete structured output.

The search space,  $\mathcal{S}_p$  is a 2-tuple  $\langle I, A \rangle$ , where  $I$  is the initial state function, and  $A(s)$  is a function that gives the set of allowed actions from a given state. Given the actions

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**Algorithm 1** Easy-first inference algorithm with learning option. When the flag *learn* is set, the algorithm performs one online training iteration on the given training example.

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1: input : Structured input  $x$ , parameter-vector  $w$ , learning option
   learn with ground truth output  $y$ , cumulative weight  $w_{sum}$ 
2:  $s \leftarrow I(x)$ 
3: TERMINATE  $\leftarrow False$ 
4: while not TERMINATE do
5:    $a_p \leftarrow \arg \max_{a \in A(s)} w \cdot \phi(a)$ 
6:   if learn is TRUE then
7:      $G(s) \leftarrow \mathcal{O}(s, y)$ 
8:      $B(s) \leftarrow A(s) - G(s)$ 
9:     if  $a_p \in B(s)$  then
10:       $w \leftarrow \text{UPDATE}(w, G(s), B(s))$ 
11:       $w_{sum} + = w$ 
12:     end if
13:      $a_p \leftarrow \text{ChooseAction}(A(s), w)$ 
14:   end if
15:    $s \leftarrow \text{Apply } a_p \text{ on } s$ 
16:   if Terminal( $s$ ) or  $a_p = HALT$  then
17:     TERMINATE = True
18:   end if
19: end while
20: output: If learn is TRUE return  $w$  and  $w_{sum}$  else return  $s$ .

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$A(s)$  from a state  $s$ , we consider any action  $a \in A(s)$  that results in a state with less loss as a *good action*; otherwise, it is a *bad action*. Within the Easy-first framework, it is typical to encounter states that have more than one good action. We denote the set of all good actions in state  $s$  as  $G(s)$  and the set of all bad actions as  $B(s)$  ( $G(s) \cup B(s) = A(s)$ ).

The second element, the action scoring function  $f$ , evaluates all actions in  $A(s)$  and guides the search to incrementally produce the structured output. In this work, we consider linear functions  $f(a) = w \cdot \phi(a)$ , where  $w$  is the weight vector and  $\phi(\cdot)$  is a predefined feature function. Given a structured input  $x \in \mathcal{X}$  and weight vector  $w$ , the Easy-first inference procedure, illustrated in Algorithm 1 (*learn* = FALSE), greedily traverses the search space  $\mathcal{S}_p$ . In any state  $s$ , the scoring function  $f$  is applied to evaluate the quality of each action  $a \in A(s)$ . The action with the highest score is executed. This process is repeated until a terminal state is reached (for problems with a natural notion of terminal states, e.g., dependency parsing) or a HALT action is chosen (for problems like coreference resolution where we need to learn when to stop) and the predicted output is returned.

The success of the Easy-first framework hinges upon the ability to choose a good action in each decision step. Hence, the *learning goal* within the Easy-first framework is to learn a weight vector  $w$  such that the highest scoring action in each step is a *good action*. Toward this goal, a general online training procedure is described in Algorithm 1 (*learn* = TRUE). In any given state  $s$ , we assume that there exists an oracle  $\mathcal{O}$  that can identify  $G(s)$  (line 7), the set of all *good actions* given the current state and the ground truth output  $y$ . If the current highest scoring action  $a_p$  is a good action, there is no need to update weights. Otherwise, the weights are updated (lines 9-12). A ChooseAction procedure is then called to select the next action (line 13), and we transit to the next

search state. This is repeated until the termination condition is met (line 16). Algorithm 1 (*learn* = TRUE) presents the procedure for one training iteration on a single training example  $(x, y)$ . This is typically repeated for every training example for multiple iterations, and the updated weights are accumulated along the way (line 11) and averaged at the end of training (to avoid overfitting) to be used for inference.

There are two elements that need to be specified in this basic training procedure. First, how to perform the update (line 10), which is the main focus of this paper. Second, how to choose the next action, which determines the training trajectories (line 13). Two types of approaches have been pursued in the literature for this purpose: on-trajectory training, which always chooses an action in  $G(s)$  (e.g., the highest-scoring action in  $G(s)$ ), and off-trajectory training, which always chooses the highest-scoring action based on the current scoring function even when it is a bad action. In this work, we consider both types of training trajectories.

### A baseline update strategy

Now we introduce a popular update strategy widely employed in prior Easy-first work (Goldberg and Elhadad 2010; Stoyanov and Eisner 2012). This strategy aims to update the weights so that one of the good actions will score the highest. To achieve this, it uses a simple heuristic by focusing on the highest scoring good action, referred to as  $g^*$ , and the highest scoring bad action, referred to as  $b^*$ , and adjusting the weights to increase  $f(g^*)$  and decrease  $f(b^*)$ . For this reason, we refer to this method as Best Good Best Bad (BGBB). The specific update rule for BGBB is:

$$w \leftarrow w - \eta \cdot (\phi(b^*) - \phi(g^*)), \quad (1)$$

where  $\eta$  is the learning rate. This update is typically done repeatedly for a fixed number of iterations or until a good action is scored the highest. In each iteration,  $g^*$  and  $b^*$  are re-evaluated. While this heuristic update has been widely applied (Goldberg and Elhadad 2010; Stoyanov and Eisner 2012), it has a number of problems. Although it updates the weights in a direction that promotes a good action and demotes a bad action, there is no guarantee that the final goal (ranking a good action above all bad actions) can actually be achieved. Very frequently, even after a large number of iterations, the updated weights can still choose a bad action. In some cases, there may not exist a weight vector that ranks a good action higher than all bad actions. In such cases, the effect of the heuristic update rule is unclear, because it lacks an explicit optimization objective.

Note that easy-first can be viewed as a greedy instantiation of the *LaSO* framework (Daume III and Marcu 2005; Xu, Fern, and Yoon 2009), a search-based structured prediction framework that is applicable to both greedy and non-greedy (beam search) search procedures. Most existing work on application of *LaSO* considers a strict left-to-right ordering of the search space, but is equally applicable to an unordered search space, which is used by Easy-first. *LaSO* weight updates are commonly done by promoting an average good action against an average bad action, which we empirically have observed to be inferior to BGBB, thus is not considered in this work.

## Proposed Method

In this section, we formulate the learning problem within Easy-first as an optimization objective and introduce a Majorization Minimization algorithm to optimize it. Our goal is to learn a linear scoring function  $f$  such that in any given state  $s$  a good action is scored higher than any bad action. This goal can be captured by the following set of constraints:

$$\max_{a \in G(s)} f(a) > f(b) \quad \forall b \in B(s) \quad (2)$$

That is, the score of the highest scoring good action needs to exceed the score of any bad action. If we identify a weight vector  $w$  that enables  $f$  to satisfy these constraints for a given  $s$ , then Easy-first would choose a correct action in state  $s$ . Because it is not always possible to find a  $w$  that satisfies all the constraints, we introduce the following average hinge loss function to capture them as soft constraints.

$$L_h(w) = \frac{1}{|B(s)|} \sum_{b \in B(s)} [1 - \max_{a \in G(s)} w \cdot \phi(a) + w \cdot \phi(b)]_+ \quad (3)$$

where  $[\cdot]_+ = \max(0, \cdot)$ ,  $B(s)$  and  $G(s)$  denote the set of bad and good actions in state  $s$ , and  $\phi(\cdot)$  returns the feature vector representing the input action.

Additionally, the weights should be only updated as much as necessary to satisfy the constraints. This is inspired by passive-aggressive Perceptron training (Crammer et al. 2006) and avoids overly aggressive updates leading to overfitting. Combining the two parts, our objective can be described as follows ( $w_0$  is the current weight prior to update):

$$\arg \min_w \lambda \|w - w_0\|^2 + \frac{1}{|B(s)|} \sum_{b \in B(s)} [1 - \max_{a \in G(s)} w \cdot \phi(a) + w \cdot \phi(b)]_+ \quad (4)$$

where  $\lambda$  trades-off the two aspects of the objective.

While the hinge loss is convex, the negative max inside makes the objective non-convex. To optimize this objective, we devise an efficient Majorization Minimization (MM) algorithm (Hunter and Lange 2004) to find a local optimal solution, which is line 10 of Algorithm 1. We describe our MM algorithm in Algorithm 2.

Our optimization algorithm works in iterations. In iteration  $i$ , we create a convex surrogate objective by replacing  $\max_{a \in G(s)} w \cdot \phi(a)$  with  $w \cdot \phi(g^*)$ , where  $g^*$  is the best good action based on the current weights  $w_i$ :

$$\arg \min_w \lambda \|w - w_0\|^2 + \frac{1}{|B(s)|} \sum_{b \in B(s)} [1 - w \cdot \phi(g^*) + w \cdot \phi(b)]_+ \quad (5)$$

This convex objective is then optimized via gradient descent (line 7) to obtain a new weight vector  $w_{i+1}$ , which is then used to identify the  $g^*$  for the convex surrogate in the next iteration. This repeats until convergence (lines 9-11) or for a fixed number of iterations ( $T$ ).

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## Algorithm 2 The MM algorithm to solve Equation 4

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1: input : current parameter-vector  $w_0$ , convergence threshold  $\epsilon$ ,
    $\lambda$ , good actions  $G(s)$ , bad actions  $B(s)$ , max number of iterations  $T$ 
2: output :  $w_i$ 
3:  $i \leftarrow 0$ , convergence  $\leftarrow$  false
4:  $pObj \leftarrow -\infty$ 
5: while  $i \leq T$  and !convergence do
6:    $g^* \leftarrow \arg \max_{a \in G(s)} w_i \cdot \phi(a)$ 
7:    $w_{i+1} \leftarrow$  solve Equation 5 via gradient descent
8:    $cObj \leftarrow$  evaluate the objective in Equation 4
9:   if  $cObj - pObj \leq \epsilon$  then
10:     convergence  $\leftarrow$  true
11:   end if
12:    $pObj \leftarrow cObj$ 
13:    $i++$ 
14: end while

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It is easy to verify that Equation 5 is an upper bound to the original objective and is tight at the current weights  $w_i$ , which guarantees that our algorithm will monotonically decrease the objective until converging to a local minimum.

We omit the details of the gradient descent subroutine for solving Equation 5. However, it is worth noting that each step of the gradient descent procedure corresponds nicely to a single update step of the Best Good Best Bad approach (Equation 1). In particular, each gradient descent step performs the following:

$$w \leftarrow w - \eta \left[ \lambda(w - w_0) + \frac{1}{|B(s)|} \sum_{a \in V} \phi(a) - \phi(g^*) \right], \quad (6)$$

where  $\eta$  is the learning rate and  $V$  is a subset of  $B(s)$  that contains all the bad actions that scored higher than  $g^*$ .

Comparing to Equation 1, we note two key differences. First, our update rule does not solely focus on the best bad action. Instead, it tries to suppress all the bad actions that incur constraint violations. We argue that by considering all violated bad actions at once, we avoid the jumpy behavior of BGBB from one iteration to the next and increase learning stability. The second key difference is that our update rule has the added flexibility for explicit control of aggressiveness and overfitting in updates. By tuning parameter  $\lambda$ , we can achieve a trade-off between aggressively satisfying the given constraints and conservatively staying close to the current weight. Hence, we refer to our update rule as Regularized Best Good Violated Bad (RBGVV).

Note that we can capture the easy-first learning goal with the following constraint as an alternative to Equation 2.

$$\max_{a \in G(s)} f(a) > \max_{b \in B(s)} f(b)$$

This naturally leads to the following alternative objective:

$$\arg \min_w \lambda \|w - w_0\|^2 + [1 - \max_{a \in G(s)} w \cdot \phi(a) + \max_{b \in B(s)} w \cdot \phi(b)]_+ \quad (7)$$

A similar MM procedure can be derived to solve this objective by introducing the following convex objective (fixing  $g^* = \arg \max_{a \in G(s)} w_i \cdot \phi(a)$ ) in each MM iteration:

$$\arg \min_w \lambda \|w - w_0\|^2 + [1 - w \cdot \phi(g^*) + \max_{b \in B(s)} w \cdot \phi(b)]_+ \quad (8)$$

And the gradient descent update rule for this objective is:

$$w \leftarrow w - \eta \left[ \lambda(w - w_0) + \max_{b \in B(s)} \phi(b) - \phi(g^*) \right] \quad (9)$$

In other words, in each MM iteration, we fix the best good action  $g^*$ , and update it against the best bad action in each gradient descent iteration. This update rule bears a strong similarity with BGBB as we focus on only the best bad in each update, but with passive-aggressive regularization included. We refer to this variant as RBGGB and consider it as an additional baseline in our experiments.

## Experimental Evaluation

We conduct our evaluation on two NLP problem domains: within-document entity coreference resolution and joint entity and event coreference resolution across documents.

### Baseline Methods

We compare our proposed Regularized Best Good Violated Bad (**RBGV**) approach with the commonly used Best Good Best Bad (**BGB**) update rule (Stoyanov and Eisner 2012). As discussed previously, RBGV differs from BGB in two key ways: first, each update of RBGV considers all bad actions that incur constraint violations; second, it incorporates passive-aggressive regularization. To understand the impact of these two factors, we also include in our comparison two additional methods: Regularized BGB (RBGB) as described at the end of the previous section, and RBGV with no regularization (BGVB). Below we present our experimental results for each problem domain.

### Entity coreference resolution within documents

We first consider the problem of entity coreference resolution within documents, which groups noun phrase mentions into clusters corresponding to entities. Within-document entity coreference resolution has been widely studied, and there exist many successful systems, including the Easy-first system (Stoyanov and Eisner 2012).

**Data.** For this problem, we conduct experiments on two entity coreference resolution corpora.

- **ACE04:** (NIST 2004) We employ the same training/testing partition as ACE2004-CULOTTA-TEST (Cullotta et al. 2007; Bengtson and Roth 2008). There are 443 documents in total, among which 268 documents are used for training, 68 documents for validating, and 107 documents for testing.
- **OntoNotes-5.0:** (Pradhan et al. 2012) We employ the official split for training, validation, and testing. There are 2802 documents for training; 343 documents for validation; and 345 documents for testing.

Our experiments use predicted mentions extracted by the UIUC mention detector (Chang et al. 2012). We evaluate

the coreference results using the updated version<sup>1</sup> (7.0) of the coreference scorer. Experiments on gold mentions show similar results and are not included in the paper.

**Experimental setup.** We implemented our learning algorithm based upon the Easy-first coreference system (Stoyanov and Eisner 2012). We employ the same set of features, which includes cluster features capturing cluster-level global agreement and mention-pair features capturing local configurations signifying coreferences. We also follow the same protocol for handling the “HALT” action (which serves as the terminal state when selected) as (Stoyanov and Eisner 2012). In particular, we represent the HALT action by a feature vector of all zeros except for a halt feature that is set to 1. For all other actions, we set the halt feature to zero. The learned weight of this halt feature operates as a threshold on action scores. During inference, if no merge action scores higher than this threshold, the search terminates.

We followed the setup of (Stoyanov and Eisner 2012) with a few small changes. To ensure fair comparison of the different update rules, we initialize all the methods with the zero weight vector. Another difference is that we employ five-fold cross-validation for parameter tuning for all methods. For BGB, we tune the learning rate ( $\eta \in \{10^{-1}, \dots, 10^{-5}\}$ ) and the maximum number of repeated perceptron updates ( $k \in \{1, 5, 10, 20, 50\}$ ) for each mistake step. For RBGV and RBGB, we tune the regularization parameter ( $\lambda \in \{10^{-4}, 10^{-3}, \dots, 10^3\}$ ). For MM-based method including BGVB, RBGV, RBGB, we tune the maximum number of MM iterations ( $T \in \{1, 5, 10, 20, 50\}$ ) and the maximum number of gradient descent steps ( $t \in \{1, 5, 10, 20, 50\}$ ). Note that for gradient descent, our method sets the learning rate to be one over the number of iterations. Finally, (Stoyanov and Eisner 2012) uses off-trajectory training. To remove the impact of the training trajectories, our experiments consider both off-trajectory and on-trajectory training.

**Results.** Table 1 show the results on the OntoNotes 5.0 and ACE2004 corpora. For evaluation, we compute MUC (Vilain et al. 1995),  $B^3$  (Bagga and Baldwin 1998), CEAF (Luo 2005), and CoNLL F1 (Pradhan et al. 2011), all of which were employed in the CoNLL Shared-task 2011. Note that CoNLL F1 is simply the average F1 values of the other three metrics.

From the results, we can see that our proposed approach (RBGV) consistently outperforms BGB for both corpora. In addition, we also observe that the unregularized version of our method (BGVB) also outperforms BGB, although with a slightly smaller margin. Similarly, our proposed method RBGV also outperforms regularized BGB (RBGB). For these three comparisons, statistical significance tests using the Paired bootstrap resampling approach (Koehn 2004) indicate that the performance differences we observe are statistically significant in all four measures.

These results collectively indicate that the performance gain of our proposed method over baseline BGB is not dominated by a single factor of using regularization or considering all violated bad actions. Rather, both factors contribute to the observed performance improvement. We no-

<sup>1</sup><http://code.google.com/p/reference-coreference-scorers/>

ALGORITHM	MUC	BCUB	CEAF <sub>e</sub>	CoNLL
<b>Results on OntoNotes 5.0 corpus.</b>				
On-Traj-RBGVB	67.51	52.05	52.46	57.34
On-Traj-BGVB	67.12	52.11	49.79	56.34
On-Traj-RBGBB	66.93	51.71	47.92	55.52
On-Traj-BGBB	66.72	50.33	47.32	54.79
Off-Traj-RBGVB	69.71	52.75	52.05	58.17
Off-Traj-BGVB	69.35	51.31	50.07	56.91
Off-Traj-RBGBB	67.55	50.97	48.82	55.78
Off-Traj-BGBB	66.02	50.76	48.61	55.13
<b>Results on ACE 2004 corpus.</b>				
On-Traj-RBGVB	51.09	69.97	48.08	56.38
On-Traj-BGVB	49.65	66.87	45.99	54.17
On-Traj-RBGBB	47.87	67.21	45.45	53.51
On-Traj-BGBB	47.71	64.67	41.55	51.31
Off-Traj-RBGVB	51.25	72.61	48.40	57.42
Off-Traj-BGVB	50.79	71.43	47.70	56.64
Off-Traj-RBGBB	49.23	70.14	46.77	55.38
Off-Traj-BGBB	48.91	68.21	46.47	54.53

Table 1: Results on within-document coreference corpora with predicted mentions. Metric values reflect version 7 of the CoNLL scorer.

ALGORITHM	MUC	BCUB	CEAF <sub>e</sub>	CoNLL
On-Traj-RBGVB	66.91	50.85	49.76	55.84
On-Traj-BGVB	65.58	49.78	49.13	54.83
On-Traj-RBGBB	64.49	49.04	47.58	53.70
On-Traj-BGBB	62.45	45.71	44.87	51.01
Off-Traj-RBGVB	66.67	51.8	51.21	56.56
Off-Traj-BGVB	66.19	50.87	50.43	55.83
Off-Traj-RBGBB	65.97	50.73	48.92	55.20
Off-Traj-BGBB	61.9	44.55	43.04	49.83
Lee et al.	66.4	50.99	49.83	55.74

Table 2: Results for cross-document joint entity and event coreference resolution with predicted mentions.

ticed that the performance gains mostly came from improved recall. In the next section, we further explore the performance differences between RBGVB and BGBB.

Note that the best performance we achieved on OntoNotes (58.17 as measured by CoNLL F1) is approximately 3% lower than the current state-of-the-art on this corpus (Durrett and Klein 2013). It is important to note that our results are not directly comparable to that of (Durrett and Klein 2013), which solves coreference resolution in a left-to-right order and uses different feature designs. By incorporating more advanced features, we expect our results to further improve.

### Joint entity and event coreference across documents

Cross-document joint entity and event coreference resolution is a challenging problem that involves resolving the coreferences for entities (noun phrases) and events (verbs) across multiple documents simultaneously.

**Data.** We employ the benchmark EECB corpus (Lee et al. 2012) for our experiments. EECB contains 482 documents

clustered into 43 topics. We use the same split for training, validation, and testing as Lee et al. (2012). Out of 43 topics, 12 topics are used for training, 3 topics for validation, and 28 topics for testing. We conduct experiments on predicted mentions. The predicted mentions are extracted using the same mention extraction system as Lee et al. (2012).

**Features.** We employ the same set of features as Lee et al. (2012) with two minor distinctions. First, in addition to the merge actions, we introduce the HALT action to serve the role of a terminal state for Easy-first search, following Stoyanov and Eisner (2012). Another minor distinction is that due to non-availability we employed a different semantic role labeling (SRL) system, which is trained on both NomBank and PropBank (Johansson and Nugues 2008).

**Comparison to state-of-the-art.** In addition to the three baselines (BGBB, RBGBB, BGVB) mentioned before, we compare our RBGVB approach with the current state-of-the-art cross-document joint entity and event coreference system by Lee et al. (2012).

**Experimental setup.** We build our experiments on top of the Stanford multi-pass sieve system (Raghuathan et al. 2010). For all methods, we employ the same set of features and the same initial processing step to the noun-phrase mentions as described by Lee et al. (2012). We set up our experiments to closely resemble the experiments by Lee et al. (2012). The parameters of RBGVB, BGVB, and RBGBB ( $\lambda$ , MM iterations  $T$ , and gradient descent iterations  $t$ ) and BGBB (learning rate  $\eta$  and maximum updates per iteration  $k$ ) are tuned with five-fold cross-validation within the training set using the same range of values specified for the within-document coreference tasks. For all methods, we tune the halt feature using the validation set to determine the stopping condition for inference. For the method of Lee et al. (2012), we employ the implementation provided by the authors and follow the parameter setup suggested in the original paper.

**Results.** Our experiments consider both on-trajectory and off-trajectory training. Lee et al. (2012) performs offline training, where the training examples can be viewed as collected in an off-trajectory fashion (not restricted to taking good actions during training). Thus it is omitted from comparison for the on-trajectory setting. We measure the performances using the same set of metrics as for within-document entity coreference (MUC,  $B^3$ , CEAF, CoNLL F1). We evaluate the results by employing the most up-to-date (Version 7) CoNLL evaluation software<sup>2</sup>.

We present the results for predicted mentions in Table 2 by evaluating both entity and event clusters jointly. First, we observe that our proposed method (RBGVB) outperforms the baseline BGBB on all measures for both on-trajectory and off-trajectory training. We also observe that RBGVB is consistently better than regularized BGBB (RBGBB). Comparing unregularized BGVB and BGBB, we again see a clear win for BGVB. These differences are consistent with what we have observed for the within-document tasks and are statistically significant according to paired bootstrap sampling test. Finally, comparing the performance of RBGVB to that

<sup>2</sup>Lee et al. (2012) used V4 of the evaluation software. Thus our results do not exactly match their reported numbers.

of Lee et al. (2012), we see a very small improvement and statistical testing indicates that the difference is only significant for the CEAF measure. This suggests that our method is comparable to the current state-of-the-art on this corpus.

Approach	Total Steps	Mistakes	Recoveries	Percentage
RBGVB	50195	16228	4255	0.262
BGGB	50195	11625	4075	0.351

Table 3: Training statistics on the ACE 2004 corpus.

### Summary of results

Our results on both domains demonstrate that our proposed RBGVB achieves statistically significant improvements over both BGGB and Regularized BGGB (RBGGB) across the board. The performance difference is more pronounced for the cross-document joint coreference problem for which our method consistently outperforms BGGB, sometimes by a large margin. Additionally, removing the impact of the regularizer, we observe that BGVB also achieves statistically significant improvements over BGGB.

### Discussion

There are two key distinctions between RBGVB and the BGGB update rule. First, BGGB considers only the best-scoring bad action in its update, whereas our method considers all bad actions that are causing constraint violations (in Equation 2) in each update. Second, our method follows a passive-aggressive strategy to discourage overly-aggressive updates. Our hypothesis is that these distinctions allow us to introduce more stability in learning and help avoid overfitting to specific bad actions encountered during training.

Approach	Mean	Variance	STDEV
RBGVB	0.87	0.0047	0.069
BGGB	0.82	0.0064	0.080

Table 4: Global performance of the learned weights on the ACE 2004 training corpus.

To shed some light on this hypothesis, we take a closer look at the effect of the updates during training. To avoid the impact of noisy mentions, we conduct this set of experiments on gold mentions and focus on within-document coreference and on-trajectory training. We collected some interesting statistics during five iterations of training for RBGVB and BGGB on the ACE2004 corpus, which are presented in Table 3. The second column of the table records the total number of search steps, which are the same for both methods with on-trajectory training. The third column shows the number of mistakes (bad actions chosen during search) encountered during training, each incurring a round of updates. The next two columns show the number and percentage of times that the update is successful (“recoveries”, where the highest-scoring action is good after update).

We were surprised to note that our method (RBGVB) is significantly less successful at correcting mistakes (26% for

BGVB vs. 35% for BGGB). How could it be less effective in correcting the mistakes but more effective overall? The explanation lies in the passive-aggressive element of our objective, which explicitly encourages small changes to the weights, sometimes at the expense of not satisfying all the constraints. This explains why our method tends to fail more at correcting the mistakes, but does not provide an answer to why its overall performance tends to be better.

To answer this question, we further examine the quality of the weights obtained by both methods in a global setting. That is, we recorded all the weights that are produced by the two learning algorithms and evaluated how well each weight can guide the greedy search on the training set. To do this, we generated some sample search trajectories on the training data, and at each search step evaluated the learned weights to choose actions. If a weight-vector chose a good action, it was considered a correct decision. For each method, we computed the percentage of correct decisions made by all of the learned weight-vectors, averaged across five randomly-generated search trajectories. The mean and variance are reported in Table 4. The results show that the weights learned by RBGVB have consistently better global performance and smaller variance. This suggests that by satisfying more local constraints, BGGB is indeed suffering from overfitting, to which our method is less prone.

### Conclusions and Future Work

We proposed a novel online learning algorithm for the Easy-first framework. By formulating the learning problem as an optimization objective, we capture the essence of the learning goal for Easy-first: select the best scoring action at each search state while avoiding overly-aggressive updates. Experiments on two NLP domains, within-document coreference resolution and cross-document joint entity and event coreference resolution, showed that our greedy learning method outperforms an existing Easy-first training method and is competitive with the current state-of-the-art for cross-document joint entity and event coreference resolution.

Easy-first makes a series of greedy local decisions, some of which can be hard without additional context, and errors can propagate to downstream decisions. Some solutions we intend to explore are to perform a search in the Limited Discrepancy Search (LDS) space (Doppa, Fern, and Tadepalli 2014b; 2014a) induced by the learned greedy policy to further improve the performance; and to improve the greedy policy by leveraging learned pruning rules (Ma et al. 2014).

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