

Booth's Algorithm

- There is more than one way to do multiplication
- An ALU can add or subtract
 - We can have: $6 = -2 + 8$
- A multiplication ($A * B$) can be performed as
 - $A * (C - D)$; where $B = C - D$
 - Assume $A=2$ and $B=6$ ($C=8$ and $D=2$)

$$2 * (8 - 2) = 12$$

Booth's Algorithm (cont'd)

0 0 1 0 two

0 1 1 0 two

0 0 0 0 shift (0)

0 0 1 0 add (1)

0 0 1 0 add (1)

0 0 0 0 shift (0)

0 0 0 1 1 0 0 two

Booth's Algorithm (cont'd)

0 0 1 0 two

0 1 1 0 two

0 0 0 0 shift (0)

0 0 1 0 sub (first 1)

0 0 0 0 shift (string of 1s)

0 0 1 0 add (last 1 in string)

0 0 0 1 1 0 0 two

Booth's Algorithm (cont'd)

0 0 1 0 two

0 1 1 0 two

Two's
complement

0 0 0 0 shift (0)

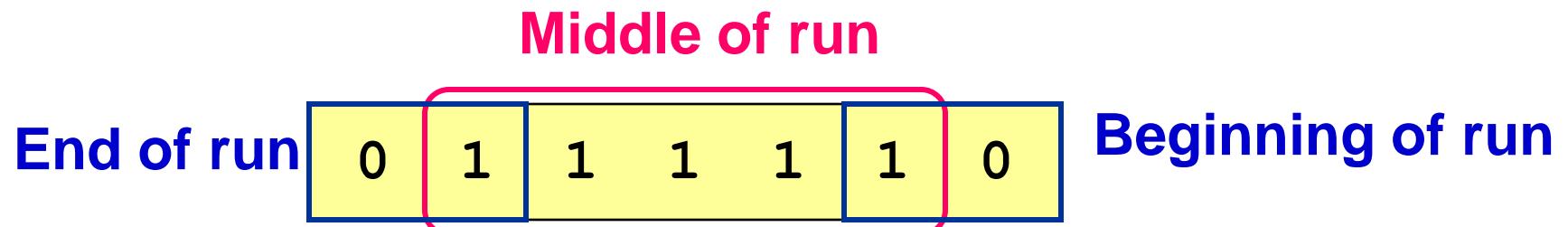
→ 1 1 1 1 1 0 sub (first 1)

0 0 0 0 shift (string of 1s)

0 0 1 0 add (last 1 in string)

0 0 0 1 1 0 0 two

Booth's Algorithm (cont'd)



Using Booth's algorithm

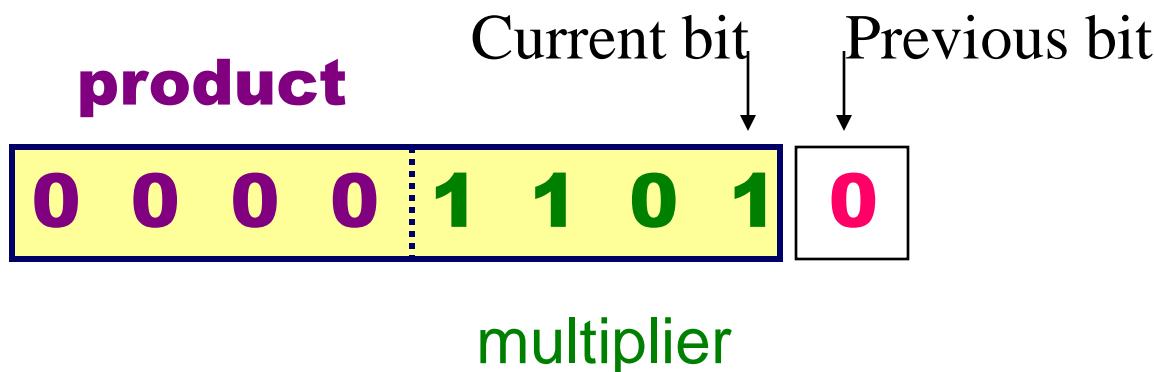
Check current bit and previous bit

- 0 0 Middle of string of 0s, NO ARITHMETIC OPERATION
- 0 1 End of string of 1s, ADD THE MULTIPLICAND
- 1 0 Beginning of string of 1s, SUBTRACT THE MULTIPLICAND
- 1 1 Middle of string of 1s, NO ARITHMETIC OPERATION

Shift product to right (1 bit)

Booth's algorithm example

$$2 \times -3 \quad \begin{array}{r} 0010 \\ \text{Multiplicand} \end{array} \quad \times \quad \begin{array}{r} 1101 \\ \text{Multiplier} \end{array}$$



Booth's algorithm example

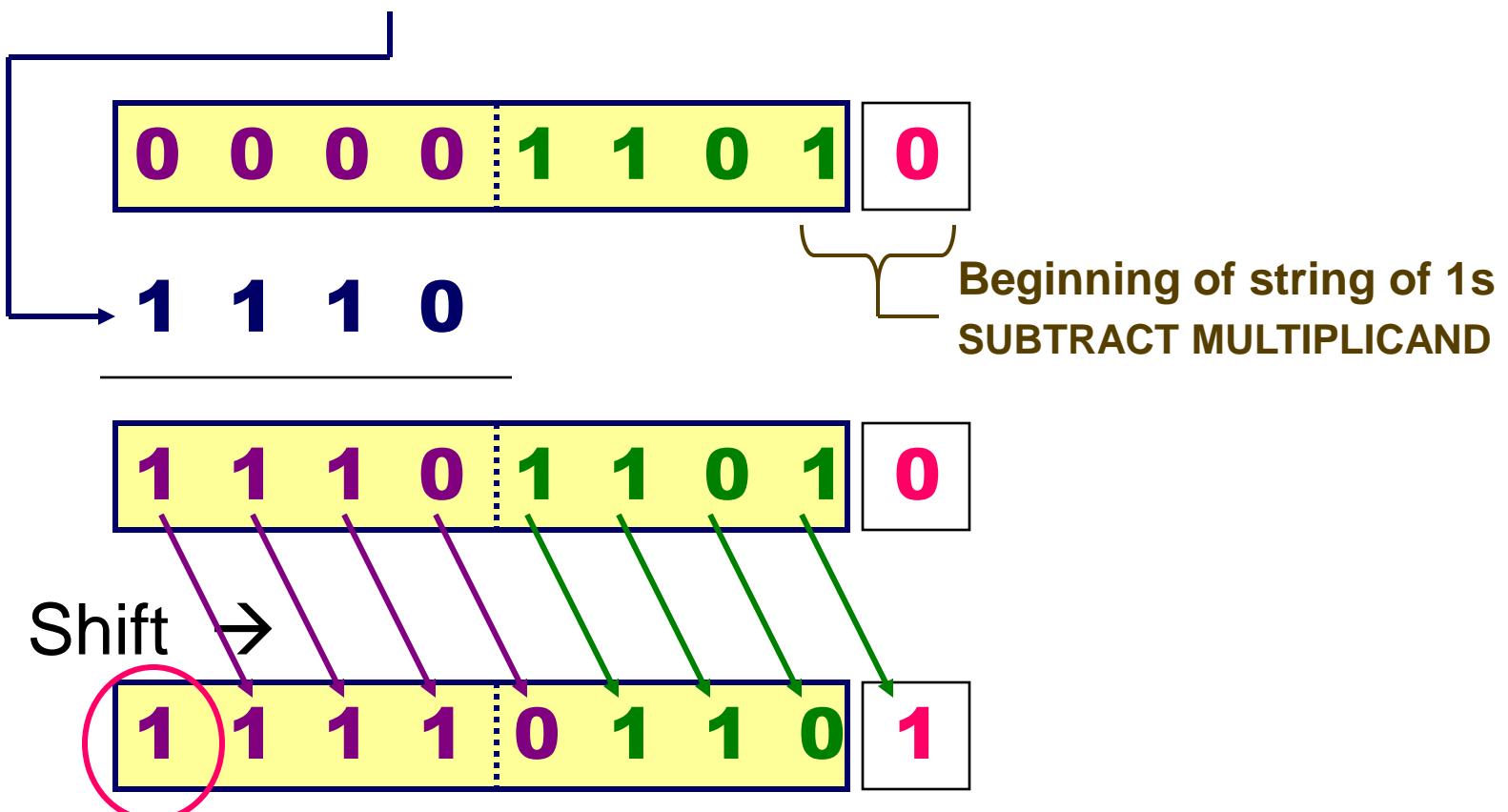
2×-3

0010

Multiplicand

$\times 1101$

Multiplier



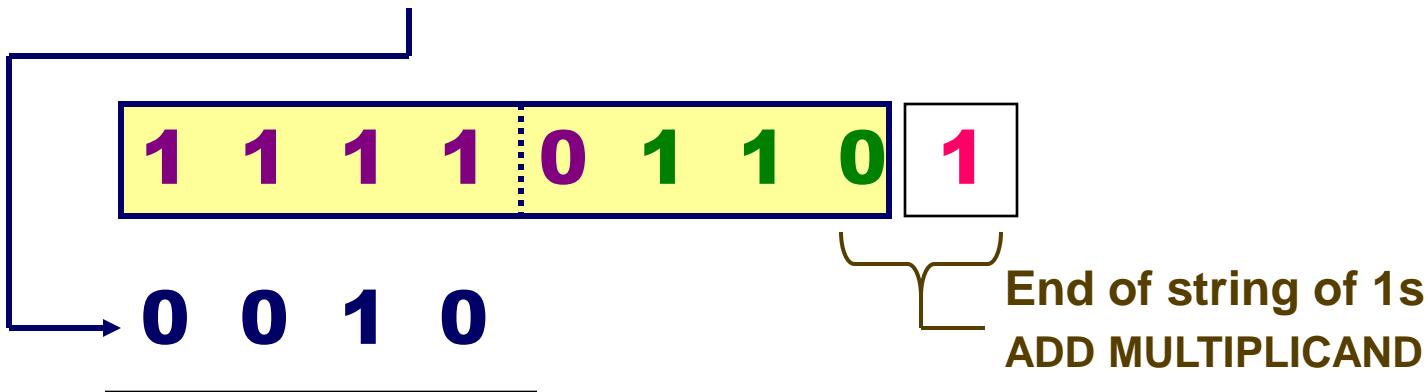
Booth's algorithm example

$$2 \times -3$$

$$0010 \quad \times \quad 1101$$

Multiplicand

Multiplier



Shift →



Booth's algorithm example

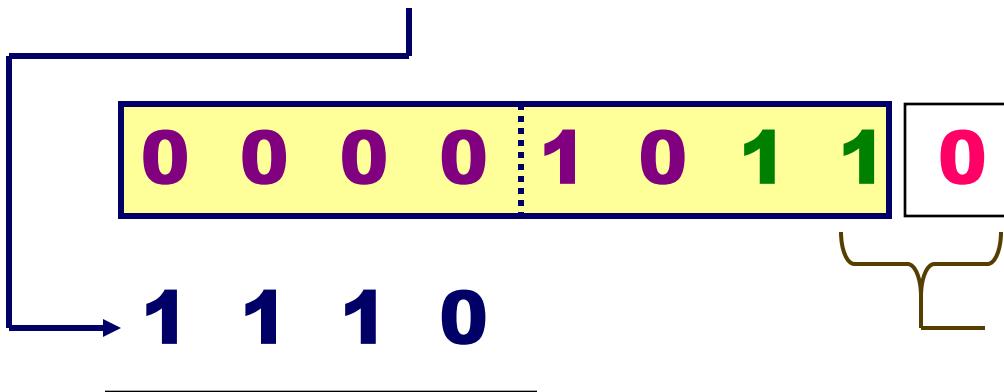
2 X -3

0010

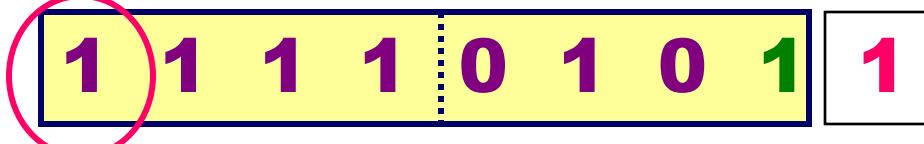
Multiplicand

x 1101

Multiplier

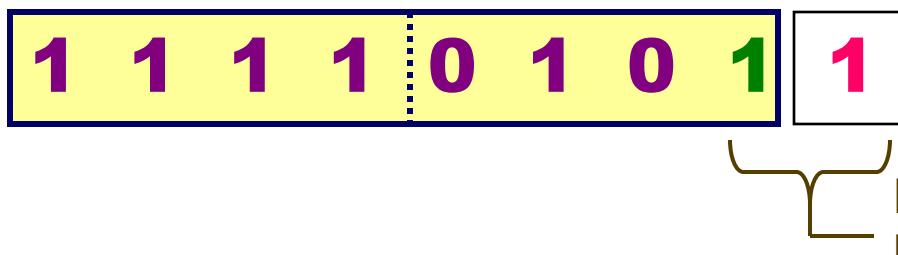


Shift →



Booth's algorithm example

$$2 \times -3 \quad \begin{array}{r} 0010 \\ \text{Multiplicand} \end{array} \quad \times \quad \begin{array}{r} 1101 \\ \text{Multiplier} \end{array}$$



Shift → (last shift)



Booth's algorithm example

1 1 1 1 1 0 1 0

Two's complement

0 0 0 0 0 1 0 1
1

0 0 0 0 0 1 1 0

8-bit multiplication

Multiplicand: 35 → 0 0 1 0 0 0 1 1

Multiplier: 79 → 0 1 0 0 1 1 1 1

0 0 0 0 0 0 0 0	0 1 0 0 1 1 1 1 0
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1 1 0 1 1 1 0 1

1 1 0 1 1 1 0 1	0 1 0 0 1 1 1 1 0
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Multiplicand:

35 → 0 0 1 0 0 0 1 1

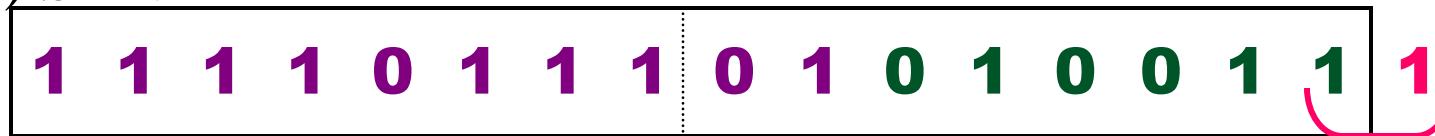
Multiplier:

79 → 0 1 0 0 1 1 1 1

(1) Shift →



(2) Shift →



(3) Shift →



(4) Shift →



Multiplicand:

35 → 0 0 1 0 0 0 1 1

Multiplier:

79 → 0 1 0 0 1 1 1 1

1 1 1 1 1 1 0 1	1 1 1 0 1 0 1 0 0 1
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0 0 1 0 0 0 1 1

0 0 1 0 0 0 0 0	1 1 0 1 0 1 0 1 0 0 1
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(5) shift →

0 0 0 1 0 0 0 0	0 1 1 0 1 0 1 0 1 0 0
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(6) shift →

0 0 0 0 1 0 0 0 0	0 0 0 1 1 0 1 0 1 0 1 0
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Multiplicand:

35 → 0 0 1 0 0 0 1 1

Multiplier:

79 → 0 1 0 0 1 1 1 1

0 0 0 0 1 0 0 0	0 0 1 1 0 1 0 1 0
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1 1 0 1 1 1 0 1

1 1 1 0 0 1 0 1	0 0 1 1 0 1 0 1 0
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(7) shift →

1 1 1 1 0 0 1 0	1 0 0 1 1 0 1 0 1 0 1
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Multiplicand:

35 → 0 0 1 0 0 0 1 1

Multiplier:

79 → 0 1 0 0 1 1 1 1

1	1	1	1	0	0	1	0	1	0	0	0	1	1	0	1	0	1	1	1	1	1	1
---	---	---	---	---	---	---	---	---	---	---	---	---	---	---	---	---	---	---	---	---	---	---

0 0 1 0 0 0 1 1

0	0	0	1	0	1	0	1	1	0	0	1	1	0	1	0	1	0	1	1	1	1	1
---	---	---	---	---	---	---	---	---	---	---	---	---	---	---	---	---	---	---	---	---	---	---

(8) shift →

0	0	0	0	1	0	1	0	1	1	1	0	0	1	1	0	1	0	1	0	0	1	0
---	---	---	---	---	---	---	---	---	---	---	---	---	---	---	---	---	---	---	---	---	---	---

$$2048 + 512 + 128 + 64 + 8 + 4 + 1 = 2765$$