EE 261

Spring 2025

Due Sunday, Apr. 13, 2025 by 11:59 p.m.

NOTE: This is only the "handwritten" portion of Homework 11. There are also problems you must do online via the Mastering site. For this handwritten portion you must submit a PDF scan of your work at Canvas. Please ensure your work is contained in a single file and is legible.

- 1. Consider the circuit shown below. The circuit is in steady state prior to t = 0.
 - (a) What is $v(t \ge 0)$?
 - (b) What is $i_L(t \ge 0)$?



- 2. Consider the circuit shown below. The circuit is in steady state prior to t = 0.
 - (a) What is $v(t \ge 0)$?
 - (b) What is i(t > 0)?



3. For the circuit below, obtain the differential equation that governs $v_2(t)$.

This can be obtained relatively easily by thinking in terms of KCL applied to the v_1 node. Express all the currents in terms of the voltages. Then, consider the current i_2 . There are two ways to express this current. One way involves Ohm's law. The other way employs the *i*-vrelationship for the capacitor C_2 . Equating these two expressions for i_2 allows you to obtain an expression for v_1 in terms of v_2 . Using that (and returning to the KCL expression) allows you to obtain a differential equation that only involves v_2 .

You should obtain a second-order differential equation with constant coefficients. We could, if we so desired, write the equation in the form:

$$\frac{d^2v_2(t)}{dt^2} + 2\alpha \frac{dv_2(t)}{dt} + \omega_0^2 v_2(t) = 0.$$

The α and ω_0 depend on R_1 , R_2 , C_1 , and C_2 (in a way that is distinct from what we have with parallel or serial *RLC* circuits), but the way in which $v_2(t)$ behaves would be no different from what we've seen before. It would be either underdamped, critically damped, or underdamped (depending on the relative sizes of α and ω_0).

Finally, you can be fairly confident that you have the right differential equation if, when you set R_2 to zero, you get a first-order differential equation with an equivalent capacitance of $C_1 + C_2$ (i.e., the time constant is $R_1(C_1 + C_2)$ if R_2 goes to zero).



- 4. For each of the following, provide the corresponding phasor. Your answer should be a complex number in *polar form*. You can use either $re^{j\theta}$ or r/θ notation.
 - (a) $-42\cos(200\pi t 0.4)$ V
 - (b) $6.2\sin(200\pi t + 35^\circ)$ mA
- 5. Given the following phasors and the information related to the frequency of that phasor, provide the corresponding time-domain representation. (It is somewhat hard to tell the difference, but the terms on the left in bold are the symbols for the phasors, e.g., V, while the terms preceding the frequency information provide the units, e.g., V is volts.)

(a)
$$V = 8e^{-j\pi/6} V$$
, $\omega = 200 \text{ rad/s}$

(b)
$$\mathbf{V} = \sqrt{2}e^{j0.25} \, \mathbf{V}, \quad f = 10 \, \mathrm{kHz}$$

(c) $\mathbf{I} = 42/\pi/6 \mathbf{A}, \quad T = 10^{-6} \mathbf{s}$